

What Makes Hiring Difficult? Evidence from Linked Survey-Administrative Data

Antoine Bertheau, Birthe Larsen, Zeyu Zhao

July 2024

We design a survey of firms and link it to Danish administrative data to yield new insights about the factors that can influence firms' hiring decisions. Several findings stand out: (1) search and training frictions are as important as labor costs in hiring decisions ; (2) search and training frictions are more likely to affect younger and smaller firms; (3) firms that prefer to hire employed rather than unemployed workers (because they believe that the unemployed have lower abilities) are more likely to report that labor market frictions alter their hiring decisions (4) firms with inaccurate beliefs of their own wages are more likely to report that labor cost considerations alter their hiring decisions.

First version: June 2023. We thank participants at the 3rd CRC TR 224 Workshop on Labor Markets, SOLE (2023), COPE (2023), EALE (2022), the University of Copenhagen, and Copenhagen Business School. We thank Jason Faberman, Fane Groes, Nikolaj Harmon, Lena Hensvik, Astrid Kunze, Thomas Le Barbanchon, Dario Pozzoli, Roland Rathelot, Morten Olsen, Christian Gormsen Schmidt, Daphné Skandalis, and Tom Zohar for their comments. Antoine Bertheau appreciates the financial support from the Danish National Research Foundation (Niels Bohr Professorship) and the Economic Policy Research Network (EPRN). Marianna Kudlyak and Morten Bennedsen contributed to the development of the survey questions that we use in this paper. We thank Mengqi Li and Konrad Juel Thide for their excellent research assistance, Christian Gormsen Schmidt for providing us with the vacancy data, Jakob Roland Munch for providing us with the wage floors data. Bertheau: Norwegian School of Economics (NHH) (e-mail: antoine.bertheau@nhh.no). Zhao: University of Copenhagen (e-mail: zzh@econ.ku.dk). Larsen: Copenhagen Business School (e-mail: bl.eco@cbs.dk).

1. Introduction

While hiring plays a crucial role in determining the level of employment and production, there is little evidence of how firms make their hiring decisions. Presumably, the decision to post a vacancy can be influenced by several factors, such as labor costs, uncertainty, or different forms of labor market friction. Which factors do actually matter? And do they vary across firms? Despite the high stakes of these questions, how employers search and make their hiring decisions is far less understood than the determinants of worker job search.

Recent literature has made progress in terms of understanding some aspects of hiring behaviors using vacancy data. For instance, it is well-documented that the job-filling rate for vacant positions varies with firm growth rate (e.g., Davis, Faberman, and Haltiwanger (2013); Bagger, Fontaine, Galenianos, and Trapeznikova (2022)). However, such data are less suited to document how firms make hiring decisions as those data solely record firms that decided to open a vacancy.

This paper helps to fill this void by surveying Danish firms on factors altering their hiring decisions. Our survey collects responses from over 2,000 firms, which are a representative sample of the population of firms. We ask firms about the relevance of several hiring factors that can discourage them from hiring despite potential needs. We distinguish between skill shortages, labor costs, search time, training time, and economic uncertainty.¹ By linking the survey to administrative datasets, we then associate the different factors with firm characteristics (e.g., firm size, age, productivity). Besides their characteristics, we analyze the role of firms' beliefs. We first assess whether firms' belief about hiring job seekers with different statuses (those already employed and those who are unemployed) is associated with factors altering firms' hiring decisions. We then investigate whether firms' labor cost concerns are related to firms' inaccurate belief of their own wage level.²

Our findings can be summarized as follows. First, we show that search and training frictions are as important as labor costs in hiring decisions. We find that around 70% of the firms agree that the lack of qualified workers discourages them from hiring despite their potential needs (labeled "skill shortage"). Around 40% agree that job seekers ask

¹Employers must report their perceptions using a 5-point Likert scale: strongly disagree, disagree, neutral, agree, or strongly agree. Our survey includes open-ended text answers to allow employers to express their opinions on other reasons.

²We measure inaccurate belief by comparing the firm's position in the wage distribution from administrative data to their beliefs.

for a higher wage than the firm can offer (labeled "labor costs"). More than a third of the firms answer that search and matching frictions matter, and a similar percentage of respondents report that training new hires in firm-specific skills discourages them from hiring (labeled "search time" and "training time"). The uncertainty of economic activity is also a concern for more than a third of the respondents.

Second, we associate factors that influence hiring decisions with firm characteristics.³ High-wage firms are less likely to consider labor costs a hiring obstacle. However, these firms are as likely to report skill shortages being a hiring obstacle at lower wage firms. This suggests that there are labor market frictions that cannot be resolved by only increasing wages. Higher wages do not affect search or training frictions either. On the other hand, smaller and younger firms are more likely to be affected by search and matching frictions. However, they are not more likely to experience difficulties due to labor costs than larger or older firms. Our evidence suggests that hiring frictions for younger firms are potentially detrimental, as those firms typically drive job creation.

Third, we associate factors influencing hiring decisions with firms' subjective beliefs. If some firms prefer to hire already employed workers rather than unemployed ones, they may leave out an important share of job seekers, potentially altering their hiring decisions. In our survey, about a third of firms answer that they prefer to hire employed over unemployed (either because they believe that skills deteriorate during unemployment or because unemployed have lower abilities). We show that preferring employed rather than unemployed workers does make hiring difficult. Our estimates reveal that the preference for hiring the employed over the unemployed increases the probability of agreeing that skill shortage and search and training frictions discourage them from hiring by 10 to 7 percentage points.⁴ Finally, we show that firms' inaccurate beliefs about their wages are likely to alter their hiring decisions. Following Bertheau and Hoeck (2024), we define inaccurate beliefs when the firm's belief about their own wage is quite different from objective wage measures. When firms believe they offer lower wages than their peers, while the administrative data show the opposite, they are more likely to agree that labor costs discourage them from hiring.

Our results suggest that the stigma of the unemployed and firms' inaccurate belief of their wages could substantially influence firms' hiring decisions.

We conduct several tests to validate our survey and strengthen the credibility of

³Our estimates control for detailed characteristics of the market, the firm, and the respondent.

⁴Differences in abilities between employed and unemployed workers could drive the correlation. Including the difference between the predicted abilities of the employed and the unemployed from administrative data has a limited impact on the estimates.

our results. First, we show that survey responses regarding firm size and change in revenue are consistent with the same measures from the administrative data. Second, our estimates are robust when we change our baseline specification. Our estimates control for local labor market conditions that could make hiring more or less difficult across firms, detailed industry and region categories, as well as a proxy for the extent of job amenities that firms offer.

The institutional setting of the labor market, the economic context, and the representativeness of our survey limit the concern that our results are specific to Denmark in the expansion after the pandemic recession. Danish firms are not subject to stringent hiring and firing regulations, and wages are typically set at the firm level. When we conducted our survey in the summer of 2021, the Danish and the World economy entered the recovery phase. Besides, the labor market was tight, but not historically tight, as it was in 2022. Hence, the empirical case of Denmark provides access to unique data without limiting external validity.

Contribution. The core contribution of this paper is to offer the first comprehensive descriptive analysis of the factors that influence firms' hiring decisions, how they vary with firm characteristics, and how they vary with firms' subjective beliefs. We do so by collecting novel data on firms' hiring decisions linked with rich administrative data. The main difference between this paper and most of the literature is that we do not use vacancy data to study hiring behavior. Using vacancy data, it is challenging to document factors altering firm hiring decisions, which is the focus of our paper. Still, the literature has made important progress in terms of understanding some aspects of hiring behaviors (e.g. recruiting intensity, reviewed in Faberman (2020)).⁵ Documenting the factors altering hiring decisions and their variation across firm characteristics and firms' subjective beliefs is important since the majority of firms report that they have hiring difficulties in the US and Europe (see Figure A.1).⁶ By offering novel evidence on firms' hiring decisions, this paper provides a better understanding of the matching process between workers and firms. This is valuable as the demand side is less understood

⁵For US evidence, see e.g. Davis, Faberman, and Haltiwanger (2013), Mongey and Violante (2019), Forsythe and Weinstein (2021). For European evidence, see e.g., Carrillo-Tudela, Gartner, and Kaas (2022), Bagger, Fontaine, Galenianos, and Trapeznikova (2022), Mueller, Osterwalder, Zweimüller, and Kettmann (2023), Lochner, Merkl, Stüber, and Gürtzgen (2021), Carrillo-Tudela, Kaas, and Lochner (2022), Hochmuth, Kohlbrecher, Merkl, and Gartner (2021).

⁶A literature leveraging causal identification shows that hiring difficulties reduce firm growth. See Signorelli and Fontaine (2024), Le Barbanchon, Ronchi, and Sauvagnat (2024), Friedrich and Zator (2024).

than the supply side.⁷ For this reason, this paper complements the literature in several important ways.

First, to our knowledge, we are the first to compare the role of labor costs and matching frictions as factors affecting firms' hiring decisions. A closely related work is Bergeaud, Cette, and Stary (2022). They show that French manufacturing firms believe that labor shortage is a more prominent obstacle than labor costs.⁸ However, existing studies do not document the extent of search and matching frictions as we do. One key takeaway from this paper is that ex-ante and ex-post matching frictions (i.e., search and training times) are relevant factors in hiring decisions. This result is consistent with novel evidence that we provide on the expected time it takes for a new employee to be as productive as an average employee in a similar position. A quarter of firms in our survey believe it will take at least one year.⁹

Second, this paper is the first to link hiring obstacles to firms' financial situations, workforce characteristics, and labor market conditions. This unique linking of survey and administrative data yields several results. Two key findings stand out. The first key finding is that a more generous wage policy is associated with fewer hiring difficulties due to labor costs. However, our data show that paying higher wages is not associated with firms being less discouraged by skill shortages. Neither are these firms less likely to be concerned about ex-ante and ex-post matching frictions. This result suggests that labor market frictions cannot be completely resolved by only offering higher wages.¹⁰ The second key result is that search and training frictions are more likely to alter hiring decisions for younger firms. Heterogeneity on the age margin is important given the role young firms play in employment growth (Sterk, Sedláček, and Pugsley 2021). There are several explanations for this. Younger firms have a smaller network and are less capable of using referrals as hiring channels (e.g, Cahuc and Fontaine (2009)). Job seekers might also be reluctant to apply to younger firms because of low visibility and imperfect information about the quality of these firms. The paper by (Kim 2023) shows in a directed search model that a high performing young firm needs to pay a higher wage than a low performing old firm due to workers being uncertain about

⁷Recent empirical studies on job search use novel survey or job search websites (e.g.,Fluchtmann et al. (2022); Marinescu and Skandalis (2021); Faberman et al. (2022); Kircher (2022)).

⁸Bergeaud, Cette, and Stary (2022) use a survey designed by the Bank of France. However, the respondents must report their perceptions about other factors.

⁹The wording of the question is: When will the newly hired employee achieve/have achieved the same productivity as an average employee in a similar position? Please indicate the estimate in months.

¹⁰These results are consistent with Mueller, Osterwalder, Zweimüller, and Kettemann (2023). They show that wage premiums can only account for a small fraction of the variation in vacancy-filling rates across establishments.

firm's performance in a long term perspective. Future research could disentangle these channels.

Third, this paper is the first to associate hiring decisions with firms' subjective beliefs. In this part, we have two distinct and novel results to our knowledge. We find that firms' preference for hiring employed workers is associated with being more likely to report factors altering firms' hiring decisions. Interestingly, this correlation is still present once we control for the average characteristics of the employed and the unemployed workers. This finding complements and explains some of the findings of Faberman et al. (2022). They show that the job search of the employed is much more effective than that of the unemployed. Our results suggest that firms' preferences for job seekers with different labor market statuses explain some of their findings. Finally, we show that a firm's inaccurate beliefs about its wages matter at the hiring margin. This result complements a new and growing literature documenting in different settings and places that firms are not well-informed about the prevailing wages (e.g., Cullen, Li, and Perez-Truglia (2024); Bertheau and Hoeck (2024); Friedrich and Zator (2024)).¹¹

The paper is organized as follows. Section 2 describes the dataset and the institutional setting. Section 3 documents factors influencing hiring decisions and how they vary across firm characteristics. Section 4.2 documents how these factors vary across firms' subjective beliefs in our survey. Section 5 concludes.

2. Linked Firm-Level Survey-Administrative Data

The main dataset is a large-scale survey we conducted in 2021 among private sector firms in Denmark. We linked this survey to administrative datasets using unique firm identifiers. We subsequently collected information about each firm's financial situation, workforce characteristics, and the labor market conditions under which they operate.

2.1. Institutional Setting and Economic Context

Institutional setting. Hiring and layoffs are not subject to stringent regulations in Denmark, which ranks 26 out of 36 countries on the OECD employment protection index. The US is ranked 36, and most Western European countries have more stringent

¹¹Cullen, Li, and Perez-Truglia (2024) show that firms with access to a salary benchmarking tool change the wages of new hires in the US. Bertheau and Hoeck (2024), using the same survey as in this paper, show that a substantial fraction of firms have inaccurate beliefs about their own wages compared to other firms. Friedrich and Zator (2024) develop a model where firms set wages based on their beliefs, and when they underestimate market-clearing wages, labor constraints arise.

policies than Denmark.¹² For 80 percent of private sector workers, the wages are set at the firm level. For the remaining 20 percent, actual wages are set by the industry collective agreement (a practice called *normallønssystemet*), and the base wages are not modified at the firm level (Dahl, Le Maire, and Munch 2013). There is no national minimum wage in Denmark but wage floors (defined at the occupation-industry level) must be followed for inexperienced workers. Employment clauses through which firms attempt to prevent employees from being employed by other firms are prohibited.

International evidence on hiring difficulties. A concern would be that Denmark differs in hiring difficulties for some reasons. Figure A.1 indicates that this is unlikely to be the case. This figure measures hiring difficulties in Europe and the United States. These figures show that hiring difficulties are an important concern throughout the business cycle, and Danish firms have lower hiring difficulties than German firms but more difficulties than Spanish firms.

Economic context in the Summer 2021. We fielded our survey in June 2021. In the Danish context, June 2021 was an opportune time to ask about human resources strategies because the world economy and the Danish economy were on the recovery track (IMF (2021); Cazes and Salvatori (2023)). In particular, the Danish recovery started in Q2 2021 (Andersen et al. 2024).¹³ To show this, Figure A.2 reports the evolution of the labor market tightness at the national level in Denmark between 2016 and 2022. Around the time of the survey, the labor market tightness was back at its pre-pandemic level.¹⁴

Our survey was implemented during a recovery phase following a recession in a country with a flexible labor market. Due to these features, it is unlikely that any special institutional settings or economic context drives our findings.

¹²Firms adjust at hiring and separations when they face shocks (e.g, Bonin (2023); Bertheau and Vejlin (2023)).

¹³This attenuates concern regarding the external validity of our survey. Indeed, there is evidence (e.g, (Buchheim et al. 2022) that sentiments in a recession could impact hiring practices of firms. Job retention programs in Denmark were less used than in other European countries. The take up rate of the furlough scheme was lower than in other European countries (10% in Denmark, 50% in France) as the Danish scheme was less generous and flexible.

¹⁴As in Europe, Barlevy, Faberman, Hobijn, and Şahin (2024) and Autor, Dube, and McGrew (2023) show that the labor market tightness started to be unusually high in 2022 and not in 2021 in the US .

2.2. Survey Overview

Sample frame. An international consulting firm (Rambøll) conducted the online survey by sending invitation emails to firms in June 2021. The target population was all private and public limited firms (ApS, *Anpartsselskab* and A/S, *Aktieselskab*) in Denmark, excluding the agricultural and mining sectors. The coverage error, i.e., the difference between the potential pool of respondents and the target population, should be negligible since all firms in Denmark must be able to receive emails from the authorities (e.g., the tax authority). The international consulting company has access to a dataset that links legal firm identifiers to company email addresses. The survey closing date was at the beginning of August 2021, and reminders were sent in July to increase the response rate.

Invitation letter. The email contained an invitation letter stating that Rambøll was surveying on behalf of the University of Copenhagen. The invitation letter was designed to recruit as many respondents as possible to minimize selection bias. It provided useful information to respondents: the deadline for completing the survey and that it could be completed using mobile-friendly devices. The actual topic of the survey was kept vague, and simple language was used to minimize selection bias. The University of Copenhagen logo was visible, and we explained that the data generated would comply with data protection rules (see Figure A.7). An invitation letter containing this information increases the response rate (Stantcheva 2023).

Question ordering. The questionnaire starts with background questions about respondents and firm characteristics. Respondents must state their role in the firm, their knowledge of pay and employment policies, the number of employees, and the change in revenue in 2020 compared to 2019. We thereby demonstrate that the respondents know the economic situation of the firm (see Figure A.3). The survey also asks questions about firm characteristics that are unavailable in administrative data sets. The next part of the questionnaire asks questions about layoffs and wages. Using these questions, Bertheau, Kudlyak, Larsen, and Bennedsen (2023) and Bertheau and Hoeck (2024) study why firms lay off workers instead of cutting wages and firms' beliefs about wage setting. This study mainly focuses on the second part of the questionnaire, which asks questions about firms hiring decisions (Appendix B.2 reports the questionnaire).

Types of questions. Qualitative questions are reported in five answer categories to make the Likert scale manageable following common practice (Dillman, Smyth, and Christian 2014). The five categories are as follows: "Strongly agree", "Agree", "Neutral", "Disagree", and "Strongly disagree". The odd number of categories ensures that there is a middle option.

2.3. Administrative Data on Firms and Workers

We link our data to eleven additional datasets to collect information on firm-specific and market-specific characteristics that can explain responses in our survey. We report the main characteristics of the administrative data for firms and workers in this section. Appendix B.1 reports additional information.

Firm and worker characteristics. We use the dataset FIRM (*Generel firmastatistik*) which contains annual financial statements for private sector firms (excluding the agricultural and financial sectors) up until 2020. Nonfinancial information, such as firm age and industry codes, is also extracted from this dataset. Workforce characteristics are obtained from various administrative registers and are averaged at the firm level. We measure whether an employee belongs to a union, her education level, age, sex, and job tenure. In addition, we have access to a dataset that indicates whether a wage floor applies to each occupation (1-digit level) by industry (3-digit level). When at least 50% of a firm's employees are subject to wage floors, we classify this firm as being covered by wage floors. We measure the extent of non-wage job amenities using a mandatory employer survey (LONN, *Lønstatistikken*).

Aggregate labor market conditions. We use a dataset containing the universe of job vacancies posted online aggregated at the occupation-region level.¹⁵ We calculate the tightness of the labor market that applies to a firm, given its workforce composition. The tightness for firm j , denoted by θ_j , is the weighted sum of the two-digit occupation-specific ($o = 1 \dots O$) labor market tightness ($\theta_o = \frac{V_o}{U_o}$).

$$(1) \quad \theta_j = \sum_{o=1}^O w_{oj} \theta_o,$$

¹⁵Vacancies are scraped from the two largest job board platforms in Denmark (Jobnet and Jobindex). In Denmark, workers must file their occupation at the start of an unemployment spell.

where V_o and U_o are the number of vacant jobs and the number of unemployed in an occupation o . The weight is then $w_{oj} = \frac{N_{oj}}{N_j}$, which is the number of workers in an occupation (N_{oj}) over the number of workers in the firm in 2019 (N_j). We measure firm-specific tightness in 2019 due to data access constraints. Data on the number of vacant jobs and the number of unemployed in an occupation for the second quarter of 2021 is not yet available to us (recall that the survey was implemented in June 2021).¹⁶

Overall, our administrative data enable us to link hiring decisions to firm characteristics, controlling for the workforce characteristics of firms and labor market conditions.

2.4. Sample Characteristics

Sample restriction. We impose the following sample restrictions. Firms and the respondents had to i) employ at least five employees in 2019, ii) operate in the private sector, iii) have financial information, and iv) (the respondents) have sufficient knowledge of the human resources policy of the firm.¹⁷

Sample representativeness. Table 1 reports descriptive statistics for the dataset for different samples. Column 1 and column 2 show the mean of the population of firms under study and the mean in our sample, respectively. The sample overrepresents larger (33 vs. 39 employees), older (18 vs. 21), and more productive firms (EUR 88,000 vs. EUR 95,000 value added per worker). The characteristics of the employees who work for the firms we surveyed are mostly similar. We reweight our sample so that it is more similar to the population reported in column 1. We construct weights using the entropy-balancing method (see Hainmueller and Xu 2013) to match the firm size, firm age, industry composition, and region. We use these weights throughout the paper. In our reweighted sample (column 3), the differences between the sample and the population are small.

¹⁶We acknowledge that our tightness measure contains only vacancies posted online, and firms other rely on other channels for job postings (see, e.g. Carrillo-Tudela, Lochner, and Kaas (2023)). We additionally validate our firm-specific tightness measure (unreported results) using an additional firm-level survey (*Rekrutteringssurvey*). Hoeck (2023) is the first to use a firm-specific tightness measure. We use national level tightness as the labor market in Denmark is relatively small, and dividing it into regional level would increase the variation in our measure.

¹⁷Specifically, we delete respondents who respond "I only know a little about pay and employment conditions" to the question "In the following questions, we ask about pay and employment practices. How close are you to such decisions?" The two other choices for this question are: "I am responsible for pay and employment conditions". and "I am not responsible, but I know about pay and employment conditions".

TABLE 1. Descriptive Statistics Across Samples of Firms

	Firm Population (Admin. data)	Linked Survey-Admin. (Unweighted)	Linked Survey-Admin. (Weighted)
Firm characteristics			
Number of employees	32.79	38.86	32.79
Firm age	18.05	20.70	18.05
Productivity	88.09	95.13	88.09
Wage premium	-0.01	0.00	-0.01
In manufacturing (%)	14.50	18.75	14.50
In services (%)	60.00	58.77	60.00
In other sectors (%)	25.50	22.49	25.50
In Copenhagen (%)	27.66	25.69	27.66
Covered by wage floor (%)	16.20	17.24	17.10
Employee characteristics			
Female (%)	28.63	28.39	29.06
Age	40.24	42.12	40.89
Tenure (years)	4.74	5.40	4.97
Bachelor's degree and above (%)	18.94	22.46	20.83
Unionized workers (%)	55.83	60.79	57.90
Observations	21797	2059	2059

Note: This table compares firm characteristics of the sample to the population of firms. Column 1 reports the mean characteristics of the population, i.e., firms with at least five full-time employees in 2019 with financial data. Columns 2 and 3 report the mean of the unweighted and the weighted sample, respectively. See Section 2 for more information about the variables and the weights.

Overall, our final sample has a response rate of about 9.44% (2059/21797) and is relatively representative of the population.¹⁸

Validating our survey. We use two questions from our survey to validate a respondent's attention to and knowledge of the economic situation of the firm. The question on firm size is "How many employees were in the firm on May 1, 2021?" We compare the reported number to the number of employees in March 2021 in the matched employer-employee dataset (BFL). Figure A.3, Panel (a) shows that the results are similar. The

¹⁸A response rate close to 10% is relatively high in non-mandatory firm survey data. Scur et al. (2021) report that response rates range from 0.1% to 13% in recent firm surveys.

second question concerns the revenue change from 2019 to 2020. We classify firms, both in our survey and in firms' financial account data (FIRM), as unchanged, increased, and decreased. Figure A.3, Panel (b) shows that the administrative data and the survey responses align well. The figure shows that most participants know the firm's economic situation. We also use other available sources to verify specific survey questions, which we discuss in the following sections.

2.5. Regression Models

We use ordered probit models to test the relevance of several hiring obstacles. The outcome variable reports the response to our main question "What factors can discourage the firm from recruiting despite the potential need?". The outcome variable may take five different values: Strongly agree, agree, neutral, disagree, strongly disagree.

$$y_i^* = \beta \mathbf{x}_i' + \gamma_{\text{region}} + \eta_{\text{industry}} + \varepsilon_i$$

The ordered probit model includes region and industry fixed effects. We report marginal effects (multiplied by 100) where covariates are evaluated at their mean values. Therefore, estimates reported in tables are interpreted as percentage point changes.¹⁹ We report the baseline probability of agreeing with the outcome variables to enable us to measure the magnitude of the effects.²⁰

Wage premiums. To estimate firm and worker fixed effects, we estimate an AKM model (Abowd, Kramarz, and Margolis 1999) using the following specification:

$$Y_{it} = X_{it}'\beta + \alpha_i + \psi_{j(i,t)} + \varepsilon_{it},$$

where Y_{it} is the log of hourly wages of worker i in period t , X_{it} are exogenous covariates, α_i is the unobserved worker effect, $j(i, t)$ is the firm where i works at t , $\psi_{j(i,t)}$ is the unobserved firm effect, and ε_{it} is an idiosyncratic error term. We include in X_{it} an unrestricted set of year dummies, as well as quadratic and cubic terms in age fully interacted with educational attainment. The model is estimated using data from 2008 to 2019.²¹ The firm-specific wage premium $\psi_{j(i,t)}$ is reported in Table 1 (labeled "wage

¹⁹Manning (2003, Chapter 10) also uses ordered probit models in its analysis of the job-filling rate.

²⁰We additionally report some of our findings using a linear probability model.

²¹We estimate the model using a matched employer-employee dataset (IDAN) containing information about the universe of jobs, including information about total earnings and total hours worked for each

premium"). It represents the proportional wage premium (or discount) paid by firm j to all employees. Such a premium is typically interpreted as rent-sharing, efficiency-wage, or strategic wage posting behavior to attract and retain employees. The worker effect is typically interpreted as a combination of skills and other factors that are rewarded equally across firms (Card, Cardoso, Heining, and Kline 2018).

3. The Determinants of the Hiring Decision

Posting a job vacancy, i.e., the hiring decision, can be influenced by several factors, such as labor costs, uncertainty, or different forms of labor market friction. This section first documents the obstacles discouraging firms from hiring despite potential needs.

Survey question on hiring decisions. The wording of the survey question on hiring decisions is: "What factors can discourage the firm from recruiting despite the potential need?" The questionnaire makes clear that we ask about the firm and not firms in general. Respondents must report their perceptions about five possible factors. To ensure that we did not leave out any important factors, there is an additional category that asks firms to provide details of "other" factors.²² This question is directly related to the canonical Diamond-Mortensen-Pissarides (DMP) model of the labor market. When the value of recruiting is above a threshold, firms engage in searching for a worker.²³ However, empirical evidence about firm's decision to open a vacancy is rare, even though vacancy creation is key to explaining labor market fluctuations (e.g., Mercan and Schoefer (2020), Qiu (2023)).

3.1. The Relative Importance of Different Hiring Obstacles

Figure 1 reports the responses to the survey question. The most prevalent hiring obstacle is the lack of qualified candidates, which more than 70% of the firms agree with. This is the most popular answer and is almost twice as popular as the second most popular

employment relationship at the yearly frequency.

²²We find that the majority of the "other" factors are similar to or are variants of the five categories we provided in the survey. Bergeaud, Cette, and Stary (2022) exploit a firm survey designed by the Bank of France that contains a similar question. However, the respondents must report their perceptions about other factors.

²³Pissarides (2011) writes: *A job is an asset owned by the firm: if it is vacant it has some value because it can expect to recruit a worker and yield some profit in the future; if it is filled it is producing for profit. Vacant jobs are like nascent investment projects that have not started yielding a return yet. If their net value is positive, the firm can create them for profit; if it is negative, it is losing money from them, so it makes sense to close them down.*

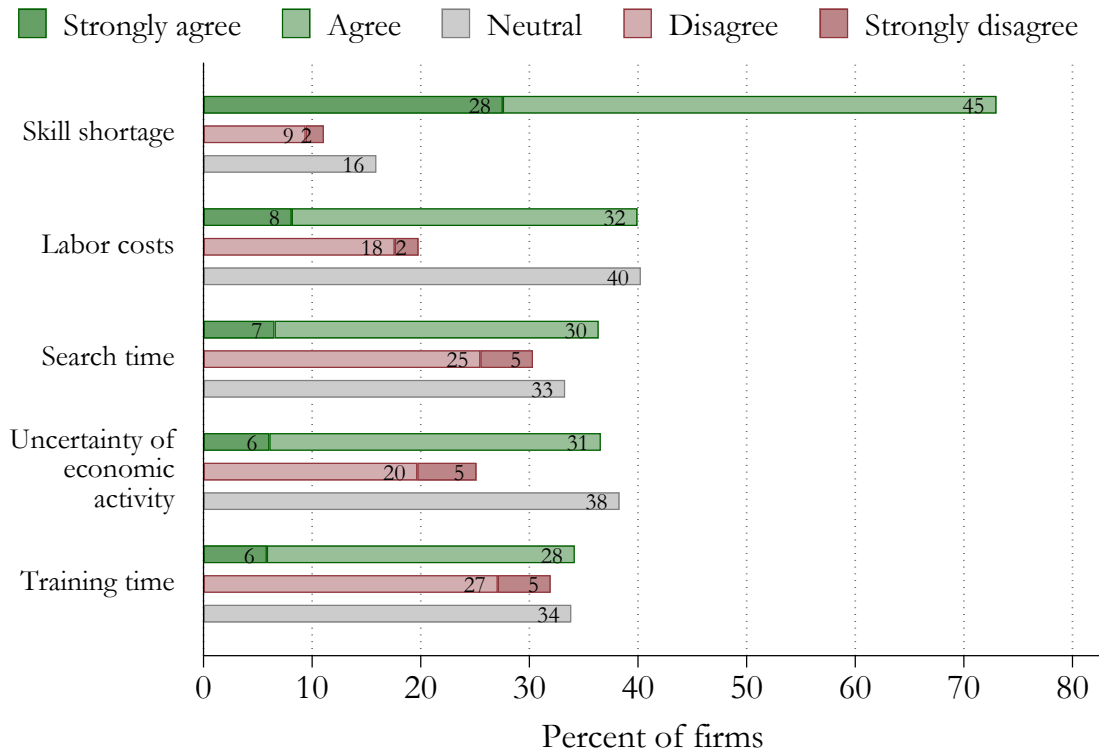
one. A significant share of the firms also agree that other factors discourage them from hiring. Around 38% of the firms agree that the jobseekers' wage expectations are too high. Around 36% of the firms agree that searching for the right employee is too time-consuming, while around 35% of the firms agree that training employees in firm-specific skills is too time-consuming. Around 37% of the firms say that uncertainty about economic activity discourages them from hiring.²⁴

The importance of training costs. Figure 1 shows that the training time for new employees is a key concern for firms. To better understand the role of training time, we ask two additional questions. First, we ask: "When recruiting an employee, which part of the hiring process is most costly in time or money?" Firms can either select "Search for candidates, conducting interviews" or "Training of new employees (either by his /her manager or colleagues). Sixty percent of firms declare that training is more costly than search. For the subsample of firms that hire in 2020, we ask: "When will the newly hired employee achieve/have achieved the same productivity as an average employee in a similar position? Please indicate the estimate in months." Respondents can choose options from zero months up to eighteen months. Around 35% of firms think it will take from zero to three months, while 25% of firms believe it will take at least one year (these results are not reported). This additional evidence is consistent with Figure 1. In sum, search and training frictions are factors that have significant effects on firms' hiring decisions.

Association between hiring obstacles. Table 2 shows the Spearman correlation between the different statements responding to this question. The most correlated factors are search and training time, with a correlation of 0.59. This correlation shows that these two non-wage labor costs will likely affect hiring decisions. Interestingly, most other difficulties are loosely correlated. For example, the correlation between labor costs and search and training costs is between 0.23 to 0.27. Other correlations vary from 0.14 to 0.29. The factor that stands out most from the others is economic uncertainty. This factor is uncorrelated with skill shortage (-0.03). Overall, table 2 shows that firms distinguish different components of hiring difficulties. It also implies that the survey results are unlikely to be driven by single underlying factors.

²⁴Figure A.4 shows that the hiring obstacles are relevant across all sectors.

FIGURE 1. Factors Altering Firms Hiring Decisions



Note: The figure reports responses to the question: "What factors can discourage the firm from recruiting despite the potential need?" The hiring obstacles are: The lack of qualified candidates (Skill shortage); Job seekers want a higher wage than the firm can offer (Labor costs); Finding and choosing the right employee is too time-consuming (Search time); Training employees in firm-specific skills is too time-consuming (Training time); The uncertainty of economic activity.

Association with labor market conditions. Next, we compare survey responses to *aggregate* measures of hiring difficulties. We measure objective benchmarks of hiring difficulties common to a similar set of firms, given their occupation mix. We consider three measures of hiring difficulties: labor market tightness (defined in Section 2.5), the percentage of unfilled vacancies (labeled "unfilled vacancies"), and the percentage of new hires who are unqualified (labeled "unqualified hires").²⁵

Table A.1 reports the results of the univariate regression of our measure of hiring obstacles on aggregate labor market conditions. Estimates are all positive, but the magnitude differs across aggregate labor market conditions measures. Reassuringly, the

²⁵Unfilled vacancies and unqualified hires are estimated from a firm-level survey (*Rekrutteringssurvey*) described in Section 2.3.

TABLE 2. Association Between Hiring Obstacles

Hiring obstacles	Skill shortage	Labor costs	Search	Training	Uncertainty
Skill shortage	1.00				
Labor costs	0.29	1.00			
Search	0.19	0.27	1.00		
Training	0.14	0.23	0.59	1.00	
Uncertainty	-0.03	0.16	0.20	0.26	1.00

Note: This table reports the correlation matrix of hiring difficulties. Hiring difficulties are the responses to the question "What factors can discourage the firm from recruiting despite the potential need?" Figure 1 shows the distribution of each response.

skill shortage estimate is three times as large as the training estimate. Meanwhile, none of these measures are correlated with economic uncertainty. This further reassures us since the current labor market conditions would have little impact on firms' hiring decisions if they are discouraged by future economic uncertainty. These results show that our survey responses indeed capture firms' hiring situations.

Additional analysis. Another concern regarding the survey question is that we ask firms to respond to a potential scenario in which they need to hire. Firms with an actual need to hire in recent periods might have different experiences or concerns regarding hiring decisions than firms without such a need. To address this, we use another question in our survey, which asks firms if they had plans to hire new employees in 2020. A total of 1072 firms answered yes to this question (52% of the baseline sample). The answer does not specify whether firms successfully hired new employees or only put an effort into recruiting people. Hence, the design of the question ensures that all firms that intended to hire, regardless of whether they were discouraged by the aforementioned factors or not, would be identified in the response. In Figure A.5, we show the responses to the hiring difficulties question but only include the firms that planned to hire in 2020. We find that the responses are virtually the same. This result shows that firms that planned to hire people in 2020 do not differ systematically in their responses from firms that did not hire, which reduces the concern that the survey responses could be different due to the actual hiring behaviors.

Theoretical framework. We check whether our results support the prediction in a search and matching model (reported in Appendix C). We examine the impact of a change in skill shortage, labor costs, search and matching friction, and uncertainty of economic activity. Consistent with our empirical results, skills shortages, which decrease worker productivity, lead to fewer vacancies. We find that higher labor costs imply a lower vacancy supply as the expected value of a job falls. The model delivers a similar negative effect on job openings if search time or training time increases. More uncertainty corresponds to a longer expected duration of a recession. As this also reduces the expected profitability of supplying a vacancy, we show this reduces vacancy supply as well. In sum, the model's predictions are consistent with our empirical results.

Relationship to other work. Haskel and Martin (2001) use UK representative establishment data and report that 35% of employers report skill shortages. Bergeaud, Cette, and Sary (2022) show that French manufacturing firms believe that labor shortage is a more prominent obstacle than labor costs. Terry and De Zeeuw (2018) examine hiring difficulties in the US and also highlight skill shortages. However, these papers do not document the extent of search and matching frictions as we do. Hence, a key takeaway from our analysis is that search and training frictions are relevant factors that typically make hiring difficult.

These results align well with and complement empirical evidence of the expected time a new employee will take to reach their *maximal* productivity (and not average, as in our survey).²⁶ Caplin et al. (2022) shows that one year of tenure is enough for about half of the jobs. On the other hand, at least three years of experience is required in more than 30% of firms. It also relates to Bertheau et al. (2022), where they show that unexpected worker death has sizeable negative consequences on firm outcomes.

Furthermore, these results support labor market models that show how predictions differ when hiring costs include both vacancy posting and training costs. Pissarides (2009) shows that the Diamond-Mortensen-Pissarides model can predict the US economy's labor market dynamics if hiring costs include a fixed component. Faccini and Yashiv (2022) show that hiring costs lead to a strong propagation of macroeconomic variables in response to technology shocks. Finally, our evidence shows that the uncertainty of economic activity discourages firms from hiring, as predicted by Den Haan, Freund, and Rendahl (2021). Overall, our analysis shows that search and training frictions are

²⁶Recall that we find that 25% of firms think that it will take at least one year for a newly hired employee to achieve the same productivity as an average employee in a similar position.

relevant factors in firms' hiring decisions.

4. Explaining The Determinants of The Hiring Decisions

The previous section documented the obstacles discouraging firms from hiring despite potential needs. We then show how they vary across firms using their characteristics measured from administrative data and firms' beliefs measured in our survey.

4.1. Hiring Obstacles, Firm and Labor Market Characteristics

The characteristics of interest are firm size, age, wage premium, labor productivity (value added per worker), and the firm's employment share in its local labor market. For easier interpretation, we normalize the characteristics of interest (i.e., we convert them to a Z-score). Table 3 shows the marginal effects from the ordered probit models discussed in the previous section. We estimate the probability that firms will agree or strongly agree with each hiring obstacle. Table 3 reports the selected firm characteristics, but all models include additional controls as well as regional and industry fixed effects. The rich firm-level data available for all firms enable us to control for heterogeneity in firm performance and workforce characteristics that are related to the characteristics of interests.²⁷ Our results are as follows.

Firm size and firm age. Some hiring obstacles are less prevalent in larger and older firms. A one standard deviation (SD) decrease in firm size is associated with a 2.97 percentage point (pp) increase in the probability that search time will be considered a hiring obstacle. Smaller firms are also more concerned about training time (3.85 pp). Similarly, younger firms are more likely to be discouraged by these two obstacles. The estimates range from -2.89 pp for search time to -3.51 pp for training time, even after controlling for wages and productivity. Our results complement studies that characterize young firms.²⁸

²⁷We include the firm ownership type (family-owned firm), capital stock, liquidity, the change in revenue and employment, educational attainment of new hires (as a proxy for upskilling), subcontracting to other companies, and the presence of a worker representative as additional controls in our regressions. We also include the average of the following employee characteristics: percentage unionized, percentage of women, average age, job tenure, percentage of workers with at least a bachelor's degree, and an index of the intensity of routine tasks.

²⁸For instance, young firms are typically matched with lower-quality workers despite being generally high-wage firms (Babina et al. 2019; Sorenson et al. 2021).

While our survey does not provide direct channels that explain why these young firms are more impacted by search and training frictions, one plausible explanation is that referrals and networks are less available to younger firms due to their smaller pool of employees. Indeed, a large body of literature shows that employee referral is one of the most used hiring methods (Topa 2011). A theoretical literature shows how social networks impact worker outcomes (e.g., Fontaine (2008), Arbex, O’Dea, and Wiczer (2019)). Firms use these networks to attract workers of better quality in hard-to-observe dimensions (Hensvik and Skans 2016).

Another possible explanation for our estimates is that it is difficult for job seekers to determine whether younger firms are good employers (i.e., they offer stable or high-quality jobs), given the lack of employment history in these firms. Using a search and matching model, Kim (2023) shows that this uncertainty affects young firms’ hiring and ultimately dampens the growth of high-potential young firms. Since young firms play a key role in employment growth (Decker et al. 2014), and the quality of the initial workers plays a significant role in young firm’s long-term success (Babina et al. 2019), our results suggest that employment policies that help firms hire should potentially place more emphasis on younger and smaller firms.

Firm-specific wage premiums and firm productivity. Next, we document the role of firms’ wage policy. In labor market models with search frictions, firms can attract more job seekers (either already employed or unemployed) by setting a higher wage than their competitors. Is a higher wage premium associated with fewer hiring obstacles? Table 3 shows that this is partly true. Indeed, high-productivity and high-wage firms are less concerned about labor costs. A one SD increase in firm productivity (wage premium) decreases the probability that the labor costs will be considered a hiring obstacle by 3.62 pp (3.94 pp). Importantly, it is worth noting that the wage premium and productivity are not associated with other obstacles, such as skill shortages, search, and training frictions. This implies that the labor market is not perfectly competitive, and that firms cannot overcome labor market frictions and fill their vacancies solely by increasing their wages. Similar insights can be drawn from Table 2, which also shows that skill shortage and labor cost difficulties are only loosely correlated. These results complement the work by Mueller et al. (2023), who find that, in Austria, the duration of a vacancy negatively correlates with the starting wage, although the effect is small in magnitude. Therefore, while more desirable employers are probably less affected by hiring obstacles, the variation does not seem to be so large that other hiring frictions do not impact those

TABLE 3. Factors Altering Firms Hiring Decisions and Firm Characteristics

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Size	1.25 (1.27)	-2.15 (1.31)	-2.97** (1.40)	-3.85*** (1.45)	-1.79 (1.21)
Age	-2.13* (1.19)	-1.94 (1.27)	-2.89** (1.29)	-3.51*** (1.25)	-1.66 (1.24)
Productivity	1.10 (1.20)	-3.62*** (1.32)	-0.86 (1.32)	-2.06 (1.29)	-5.03*** (1.38)
Wage premium	0.20 (1.18)	-3.94*** (1.19)	-0.93 (1.15)	0.74 (1.09)	-2.17* (1.17)
Local empl. share	-1.18 (1.55)	0.75 (1.51)	-5.43*** (1.88)	-1.06 (1.78)	-2.50** (1.18)
Wage floor	-7.39** (3.58)	-9.40** (3.93)	-0.92 (3.90)	0.02 (3.74)	4.02 (4.04)
<i>N</i>	2059	2059	2059	2059	2059
Probability	.73	.37	.35	.33	.36
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table shows ordered probit marginal effects of firm characteristics on the probability of agreeing with different hiring obstacles. The exact wording of the hiring obstacles is reported in Section 3.1. Firm characteristics are measured using administrative data and are normalized (i.e., convert to a Z-score), except for whether the firm is covered by wage floors (indicator). Additional controls include firm, workforce, and respondent characteristics, as well as 59 industry- and 5 region-fixed effects, and firm-specific labor market tightness (see Section 2.4). Asterisks show statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

firms. One implication of our results is that high-paying firms could potentially create more jobs and increase labor demand if there were less labor market friction.

Finally, we find that higher productivity significantly reduces the impact of economic uncertainty (5.03pp). This is consistent with Den Haan, Freund, and Rendahl (2021), who show that volatility increases the option value of waiting. It deters low-productivity firms from posting vacancies and leads to lower job creation.

Firm monopsony power. Monopsony theory suggests that the labor market in which firms operate should also impact their decisions (Manning 2021). In a more concentrated market, employer search time decreases as employers have fewer competitors. We proxy firm-level monopsony power as its employment share in its local labor market. Firms are assigned a given local labor market within a given region (5 regions) and industry (at the two-digit level).²⁹ Consistent with the theory, firms with higher monopsony power are less likely to consider search friction a hiring obstacle. The association is also strong in magnitude, as the estimates are larger than the role of firm age or firm size. Similar results and magnitudes are obtained regarding uncertainty, which may indicate that a more stable labor supply reduces the negative impact of uncertainty. Interestingly, we do not find that firms with high monopsony power are less likely to consider training time or skill shortages as hiring obstacles (consistent with our results as regards wage premiums).

Sectoral minimum wages. In Denmark, employment protection is low and does not significantly impact hiring decisions.³⁰ However, in our sample, 17% of firms are covered by wage floors at the sectoral level that set minimum wages for most of their employees. This institutional setting could lead to firms being more discouraged from hiring. However, we do not find this to be the case. Being covered by wage floors reduces the probability of firms reporting that labor cost is a hiring obstacle by 9.40 percentage points.³¹ One explanation is that wage floors provide information about the market wage, which reduces the likelihood of firms misperceiving the market wage. This result is consistent with the recent literature documenting that many firms are not well-informed about the prevailing equilibrium wages. Cullen (2024), Bertheau

²⁹This monopsony power measure differs from the firm size (or productivity) as this margin takes into account the competitiveness of the local labor market.

³⁰Our open-ended text, where employers describe other hiring obstacles, shows this. This differs from the results in Bergeaud, Cette, and Stary (2022).

³¹This result is less stable than other findings. Table A.5 restricts our sample to firms with at least ten employees, and the magnitude of this effect is similar (-8.50 pp vs. -7.39 pp), but standard errors are larger.

and Hoeck (2024) and Friedrich and Zator (2024). Being covered by wage floors also diminishes the probability that firms answer that search cost is a hiring obstacle by 7.39 percentage points. Hence, wage floors may make the firm more attractive for job search.

Heterogeneity analysis. We uncover how the average marginal effects vary with firm size, age, productivity, wage premium, and monopsony power. Figure A.6 shows the results. We evaluate the marginal effects of each individual firm and plot the average marginal effect of each decile. We show the results only when the effect of the variable is statistically significant in Table 3. Overall, the average marginal effects are larger for smaller, younger, less productive, lower wage, or lower labor market power firms. These results indicate that the chance of encountering hiring obstacles decreases faster when firms at the lower end of the distribution move up.

Additional analysis. We carry out additional analyses to ensure that our results are robust across specifications. First, we find similar results using OLS instead of ordered probit (see Table A.2).³² Remember that all regressions are weighted to ensure comparability to the firm population under study. Regressions without weights also yield similar results (see Table A.3). The main results discussed are quantitatively similar. We also address the concern that the hypothetical nature of our question could potentially bias the results, by running the main ordered probit model with only the subsample of firms that indicate that they planned to hire in 2020 (see Table A.4).³³ We obtain similar results in all the robustness tests mentioned above.

Finally, we test whether different job amenities explain our results. Firms with negative job traits might have different firm characteristics (e.g., low productivity) which could partially drive our results. We do not find this to be the case. To control for these characteristics, the regressions include the fraction of the firm's wage bill devoted to paying for non-standard working conditions. Non-standard working conditions are defined as irregular work schedules (such as night work, work on public holidays, delayed lunch, on-call and relocation) and irregular working conditions (such as outdoor work and extreme weather). We also measure the positive non-wage amenities (labeled "employee benefits"). They are defined as the value of free cars, meals, lodging, multimedia,

³²Instead of predicting the probability of agreeing, we use a quantitative scale ranging from 1 (strongly disagree) to 5 (strongly agree).

³³Note that the sample size is smaller (around 1000 observations) in Table A.4, making the magnitude of a minority of estimates differ.

taxable health insurance and treatments, canteen arrangements, and work clothes. We do not include these variables in our main analysis because the data set recording wage conditions (LONN) is only available for a subsample of firms, and including them would cut our sample size by half. The estimates are reported in Table A.5. Non-standard work conditions are positively associated with reporting that search is a hiring obstacle (2.46 pp). This result is consistent with studies showing that unfavorable job amenities are associated with a lower labor supply (e.g., Maestas et al. 2023). Despite having a much smaller sample size, how hiring obstacles vary across firms is similar in this specification. Younger firms are still more likely to be affected by similar hiring obstacles. Higher wage premiums still reduce the likelihood of reporting labor costs being an issue (-3.55 pp vs. -3.94 pp in the main specification). Taken together, these additional results provide support for our the association that we document in table 3.

4.2. Firms Hiring Decisions and Beliefs about Hiring Workers with Different Employment Statuses

So far, we have associated the factors that influence firms' hiring decisions with the characteristics of the firm and the market in which the firm operates. However, as discussed in Stantcheva (2023), beliefs can influence the decisions of workers and firms. In this and the next section, we explore two economic mechanisms that associate firms' beliefs and their hiring decisions.

Do employers who prefer to hire already employed workers perceive greater hiring difficulties? We hypothesize that employers who prefer employed over unemployed workers, either due to skill depreciation or adverse selection concerns, have a more limited pool of candidates, which could increase their hiring difficulties.³⁴ To test this hypothesis, we use the following survey question: Tell us your thoughts about hiring other firms' employees. Please express your opinion on the following statements: "we prefer to hire candidates who are employed as the unemployed lose their skills", and "we prefer to hire candidates who are employed because unemployed workers have lower abilities than those who are employed". We find a wide variation in firm beliefs about this topic in our survey. 24% of the firms believe that skills depreciate over an unemployment spell, and 23% of the firms believe that the unemployed workers are negatively selected, i.e., have lower abilities. Overall, around 30% of the respondents

³⁴Even though thoroughly understanding this relationship is beyond the scope of this paper, we nonetheless suggest a channel that can potentially explain this link.

agree with at least one of these two statements.³⁵ We then construct a dummy variable that indicates whether the respondents agree with at least one of these two statements (labeled "prefer hiring employed").

Table 4 presents our results on the association between preferring hiring employed workers and factors discouraging hiring. The specification is the same as in Table 3, except that we include the dummy variable described above. Recall that estimates are conditional on firm and labor market characteristics. This reduces the concern that tighter labor market conditions induce some firms to prefer to hire employed over unemployed workers. We also control for the difference in abilities between the employed and the unemployed at the firm level.³⁶

TABLE 4. Factors Altering Hiring Decisions and Firms' Beliefs about the Unemployed

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Prefer hiring employed	10.48*** (2.28)	9.00*** (2.38)	7.83*** (2.30)	7.29*** (2.21)	1.75 (2.23)
<i>N</i>	2031	2031	2031	2031	2031
Probability	.73	.37	.35	.33	.36
Firm characteristics	Yes	Yes	Yes	Yes	Yes
Additional controls	Yes	Yes	Yes	Yes	Yes
$\Delta E-U$ abilities	Yes	Yes	Yes	Yes	Yes

Note: The table shows ordered probit marginal effects of firms' preference for the employed over the unemployed on the probability of agreeing with different hiring obstacles. "Prefer hiring employed" is an indicator variable. Firm characteristics from Table 3 are included as controls and their estimates are reported in Table A.7. Asterisks report statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

We find that the preference for the already employed is strongly correlated with all

³⁵We show in the Appendix that firms' preference for the employed over the unemployed does indeed affect their hiring behaviors. We find that preferring the employed for either reason (skill depreciation or negative selection) is associated with an increase in the poaching rate by around 10 percentage points (see Table A.6).

³⁶This proxy is constructed using the occupational level worker effect difference, weighted by the occupation share in each firm. That is, $\Delta_{E-U, j} = \sum_{o=1}^O w_{oj} (\bar{\alpha}_o^E - \bar{\alpha}_o^U)$, where $\bar{\alpha}_o^E$ and $\bar{\alpha}_o^U$ are the mean of AKM worker fixed effects in occupation o estimated in the AKM model, and w_{oj} is the fraction of workers employed in occupation o , in firm j .

the hiring obstacles except economic uncertainty. Agreeing with at least one of the two statements is associated with a 7.29 to 10.48 pp increase in the probability of reporting hiring difficulties.

This result can be explained, perhaps, by employers' consideration of the heterogeneity of the abilities of unemployed workers. Consistent with this explanation, Darougeh (2023) shows that a subgroup of Danish unemployed workers has much lower abilities than most unemployed workers.³⁷ This explanation is consistent with the results documented by Faberman et al. (2022). They show that the job search of the employed is more effective than that of the unemployed. Our novel descriptive evidence on the firm side complements the descriptive evidence on the worker side (to our knowledge, only reported and documented by Faberman et al. (2022)). While it is also, surely to some extent, driven by the differences in worker abilities between these two groups, we also measure the difference in employers' preferences. An indication of this is that the preference measure is not associated with firm characteristics (results not shown here), and the effect on hiring behavior persists after including a firm-level measure of worker ability differences. Our evidence highlights the importance of firms' beliefs on the status of job seekers in hiring decisions.³⁸

4.3. Hiring Obstacles and Firms' Beliefs about Their Own Wages

Why do firms not raise wages to attract workers? Friedrich and Zator (2024) theoretically shows that when firms set wages based on their beliefs and underestimate market-clearing wages, it leads to labor constraints.³⁹ We investigate whether inaccurate beliefs of their own wage affect hiring difficulties. To do so, we follow Bertheau and Hoeck (2024) and use one survey question that asks firms about their beliefs about their wage policy relative to other firms. The wording of the question is as follows: "Do you think that the firm offers lower or higher wages than competing companies in your industry? Competing firms are other employers that hire people with the same abilities in your region." The respondents have five potential options: much lower, lower, about the same, higher, and much higher. We then compare their answers to firm-specific wage premiums. Bertheau and Hoeck (2024) show that a firm's beliefs about its position in

³⁷He also uses administrative data and proxy worker abilities using AKM worker fixed effects.

³⁸This evidence supports the macro-labor models that emphasize this channel. Specifically, the feedback between employed workers' search efforts and firms' vacancy creation incentive amplifies the economy's response to a negative productivity shock and generates empirically plausible declines in vacancies (see Eeckhout and Lindenlaub (2019) and Faberman et al. (2022)).

³⁹To our knowledge, Friedrich and Zator (2024) has been released after this paper.

the wage distribution correlate with its position in the firm-specific wage premium distribution. However, a substantial minority of firms misperceive their position in the wage distribution. We define a categorical variable that measures whether a firm underestimates or overestimates its' own wage in the wage distribution.

Table 5 shows that inaccurate beliefs are associated with firms' hiring decisions. We control for firm-specific labor market tightness to alleviate the concern that a tight labor market might alter firms' beliefs about their own wage.⁴⁰

TABLE 5. Factors Altering Hiring Decisions and Wage Inaccurate Beliefs

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Underestimates own wage	-5.00* (2.88)	5.71* (2.94)	-1.95 (2.91)	-4.81* (2.76)	-0.22 (2.89)
Overestimates own wage	-0.37 (3.13)	-11.06*** (3.12)	3.64 (3.06)	1.26 (3.00)	-1.40 (3.04)
Wage premium	1.11 (1.72)	-8.33*** (1.64)	0.53 (1.63)	2.08 (1.57)	-2.54 (1.67)
<i>N</i>	2059	2059	2059	2059	2059
Probability	.73	.37	.35	.33	.36
Firm characteristics	Yes	Yes	Yes	Yes	Yes
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table reports ordered probit marginal effects of firms' inaccurate beliefs of their own wage in the wage distribution on the probability of agreeing with different hiring obstacles. Underestimating and overestimating own wage are indicator variables. The baseline category is correctly believing how a firm's wage compares to other firms. Firm characteristics showed in Table 3 are included as controls, and their estimates are reported in Table A.8. Asterisks report statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

We find that firms that underestimate their wages are 5.71 pp more likely to agree that labor costs are a hiring obstacle. This result means that firms that believe they pay lower wages than their peers, despite the administrative data showing the opposite, are

⁴⁰The specification is the same as in Table 3 except for the inaccurate belief dummy. We also define inaccurate belief using different thresholds and find the results to be similar.

discouraged from hiring due to their perceived labor costs. On the other hand, when a firm overestimates its wage in the wage distribution, this reduces the probability that it views the expected salary as a hiring obstacle. Interestingly, once we control for inaccurate beliefs, firms' wage premiums have a much stronger effect on their reported hiring difficulties regarding labor costs. A one standard deviation increase in the wage premium reduces the probability of reporting labor costs as hiring difficulties by 8.33 percentage points, in contrast to 3.94 percentage points in our main specification in Table 3. Our findings illustrate the important role played by (inaccurate) beliefs which could have significant effects on firms and labor market outcomes. It suggests an explanation for why firms use salary benchmarking (see Cullen (2024) for a literature review). These results shed new light on the role of the demand side of subjective beliefs, complementing the literature on how supply-side subjective beliefs affect labor market outcomes.

5. Conclusion

This paper provides novel insights into the determinants of hiring decisions. We do so by designing a firm survey sent out to Danish firms which we match with administrative datasets. We ask firms about the factors that can discourage them from hiring despite potential needs. We show how these factors vary with firm characteristics and with firms' subjective beliefs. Recent studies use vacancy data and have made great progress in understanding hiring behaviors (see, e.g., Faberman (2020)). However, more is needed to know what factors influence hiring decisions and how they vary across firms.

Our findings are as follows. Ex-ante and ex-post matching costs (i.e., search and training time) are as important as labor costs. These frictions are larger for smaller and younger firms. A more generous pay policy reduces hiring obstacles related to labor costs but does not affect search and training frictions. Our survey also reveals that firms' beliefs are associated with factors altering firms' hiring decisions.

Firms that prefer to hire employed rather than unemployed workers are more likely to report that labor market frictions and labor cost considerations alter their hiring decisions. We also find that inaccurate beliefs about a firm's own wages compared to others are associated with factors altering hiring decisions.

References

- Abowd, John, Francis Kramarz, and David Margolis. 1999. "High Wage Workers and High Wage Firms." *Econometrica* 67 (2):251–333.
- Andersen, Per, Simone Bonin, Pernille Borgensgaard, Josefine Dahl-Sorensen, Saman Darougheh, Erik Grenestam, Nikolaj Hansen, Simon Hviid, and Rasmus Jensen. 2024. "The pressure on the labour market has eased after a job-intensive expansion." Danmarks Nationalbank.
- Arbex, Marcelo, Dennis O’Dea, and David Wiczer. 2019. "Network Search: Climbing the Job Ladder Faster." *International Economic Review* 60 (2):693–720.
- Autor, David, Arindrajit Dube, and Annie McGrew. 2023. "The Unexpected Compression: Competition at Work in the Low Wage Labor Market." *NBER Working Paper (31010)* .
- Babina, Tania, Wenting Ma, Christian Moser, Paige Ouimet, and Rebecca Zarutskie. 2019. "Pay, Employment, and Dynamics of Young Firms." Working Paper.
- Bagger, Jesper, Francois Fontaine, Manolis Galenianos, and Ija Trapeznikova. 2022. "Vacancies, Employment Outcomes and Firm Growth: Evidence From Denmark." *Labour Economics* 75:102103.
- Barlevy, Gadi, R Jason Faberman, Bart Hobijn, and Ayşegül Şahin. 2024. "The Shifting Reasons for Beveridge Curve Shifts." *Journal of Economic Perspectives* 38 (2):83–106.
- Bergeaud, Antonin, Gilbert Cette, and Joffrey Stary. 2022. "Recruitment Difficulties and Firms’ Characteristics: An Analysis of French Company Data." *Economics and Statistics*.
- Bertheau, Antoine, Pierre Cahuc, Simon Jäger, and Rune Vejlin. 2022. "Turnover Costs: Evidence from Unexpected Worker Separations." *Working Paper* .
- Bertheau, Antoine and Christian Philip Hoeck. 2024. "Firm Beliefs About Wage Setting." Mimeo.
- Bertheau, Antoine, Marianna Kudlyak, Birthe Larsen, and Morten Bennedsen. 2023. "Why Firms Lay Off Workers instead of Cutting Wages : Evidence from Matched Survey-Administrative Data." SSRN Working Paper.
- Bertheau, Antoine and Rune Vejlin. 2023. "Job Ladders by Firm Wage and Productivity." SSRN Working Paper.
- Bonin, Simone Maria. 2023. "The Long-Lasting Effect of a Credit Crunch: Firms’ Adjustments During the Great Recession in Denmark." SSRN Working Paper.
- Buchheim, Lukas, Jonas Doovern, Carla Krolage, and Sebastian Link. 2022. "Sentiment and firm behavior during the COVID-19 pandemic." *Journal of economic behavior & organization* 195:186–198.
- Cahuc, Pierre and François Fontaine. 2009. "On the efficiency of job search with social networks." *Journal of Public Economic Theory* 11 (3):411–439.
- Caplin, Andrew, Minjoon Lee, Søren Leth-Petersen, Johan Sæverud, and Matthew Shapiro. 2022. "How Worker Productivity and Wages Grow with Tenure and Experience: The Firm Perspective." NBER Working Paper (30342).
- Card, David, Ana Rute Cardoso, Jörg Heining, and Patrick Kline. 2018. "Firms and Labor Market Inequality: Evidence and Some Theory." *Journal of Labor Economics* 36 (S1):S13–S70.

- Carrillo-Tudela, Carlos, Hermann Gartner, and Leo Kaas. 2022. "Recruitment Policies, Job-Filling Rates and Matching Efficiency." *Journal of the European Economic Association*. Forthcoming.
- Carrillo-Tudela, Carlos, Leo Kaas, and Benjamin Lochner. 2022. "Matching through search channels." Unpublished manuscript.
- Carrillo-Tudela, Carlos, Benjamin Lochner, and Leo Kaas. 2023. "Matching Through Search Channels." .
- Cazes, Sandrine and Andrea Salvatori. 2023. "The labour market impact of the COVID-19 crisis in the Nordic countries." .
- Cullen, Zoe. 2024. "Is Pay Transparency Good?" NBER Working Paper (31060).
- Cullen, Zoe, Shengwu Li, and Ricardo Perez-Truglia. 2024. "What's My Employee Worth? The Effects of Salary Benchmarking." NBER Working Paper (30570).
- Dahl, Christian, Daniel Le Maire, and Jakob Munch. 2013. "Wage Dispersion and Decentralization of Wage Bargaining." *Journal of Labor Economics* 31 (3):501-533.
- Darougheh, Saman. 2023. "The Role of Marginal Workers in Danish Unemployment." Danmarks Nationalbank.
- Davis, Steven, Jason Faberman, and John Haltiwanger. 2013. "The Establishment-Level Behavior of Vacancies and Hiring." *The Quarterly Journal of Economics* 128 (2):581-622.
- Decker, Ryan, John Haltiwanger, Ron Jarmin, and Javier Miranda. 2014. "The Role of Entrepreneurship in Us Job Creation and Economic Dynamism." *Journal of Economic Perspectives* 28 (3):3-24.
- Den Haan, Wouter, Lukas Freund, and Pontus Rendahl. 2021. "Volatile Hiring: Uncertainty in Search and Matching Models." *Journal of Monetary Economics* 123:1-18.
- Dillman, Don, Jolene Smyth, and Leah Melani Christian. 2014. *Internet, Phone, Mail, and Mixed-Mode Surveys: The Tailored Design Method*. John Wiley & Sons.
- Eeckhout, Jan and Ilse Lindenlaub. 2019. "Unemployment cycles." *American Economic Journal: Macroeconomics* 11 (4):175-234.
- Faberman, Jason. 2020. "Recruiting Intensity." IZA World of Labor.
- Faberman, Jason, Andreas I Mueller, Ayşegül Sahin, and Giorgio Topa. 2022. "Job Search Behavior among the Employed and Non-Employed." *Econometrica* 90 (4):1743-1779.
- Faccini, Renato and Eran Yashiv. 2022. "The Importance of Hiring Frictions in Business Cycles." *Quantitative Economics* 13 (3):1101-1143.
- Fluchtmann, Jonas, Anita Glenny, Nikolaj Harmon, and Jonas Maibom. 2022. "Unemployed Job Search Across People and Over Time: Evidence From Applied-for Jobs." *Journal of Labor Economics*. Forthcoming.
- Fontaine, Francois. 2008. "Why Are Similar Workers Paid Differently? The Role of Social Networks." *Journal of Economic Dynamics and Control* 32 (12):3960-3977.
- Forsythe, Eliza and Russell Weinstein. 2021. "Recruiting Intensity, Hires, and Vacancies: Evidence from Firm-Level Data." .
- Friedrich, Benjamin and Michael Zator. 2024. "Price Discovery in Labor Markets: Why Do Firms Say They Cannot Find Workers?" Tech. rep., Mimeo.

- Hainmueller, Jens and Yiqing Xu. 2013. “ebalance: A Stata Package for Entropy Balancing.” *Journal of Statistical Software* 54 (7):1–18.
- Haskel, Jonathan and Christopher Martin. 2001. “Technology, Wages, and Skill Shortages: Evidence From UK Micro Data.” *Oxford Economic Papers* 53 (4):642–658.
- Hensvik, Lena and Oskar Skans. 2016. “Social Networks, Employee Selection, and Labor Market Outcomes.” *Journal of Labor Economics* 34 (4):825–867.
- Hochmuth, Brigitte, Britta Kohlbrecher, Christian Merkl, and Hermann Gartner. 2021. “Hartz IV and the decline of German unemployment: A macroeconomic evaluation.” *Journal of Economic Dynamics and Control* 127:104114.
- Hoeck, Christian Philip. 2023. “Wage Effects of Labor Market Tightness.” Danmarks Nationalbank Working Paper (187).
- IMF. 2021. “World Economic Outlook: Managing Divergent Recoveries.” .
- Kim, Seula. 2023. “Workers’ Job Prospects and Young Firm Dynamics.” Working Paper.
- Kircher, Philipp. 2022. “Job search in the 21st Century.” *Journal of the European Economic Association* 20 (6):2317–2352.
- Le Barbanchon, Thomas, Maddalena Ronchi, and Julien Sauvagnat. 2024. “Hiring Difficulties and Firms’ Growth.” *Working Paper* .
- Lochner, Benjamin, Christian Merkl, Heiko Stüber, and Nicole Gürtzgen. 2021. “Recruiting intensity and hiring practices: Cross-sectional and time-series evidence.” *Labour Economics* 68:101939.
- Maestas, Nicole, Kathleen Mullen, David Powell, Till von Wachter, and Jeffrey Wenger. 2023. “The Value of Working Conditions in the United States and the Implications for the Structure of Wages.” *American Economic Review* 113 (7):2007–47.
- Manning, Alan. 2003. *Monopsony in Motion: Imperfect Competition in Labor Markets*. Princeton University Press.
- . 2021. “Monopsony in Labor Markets: A Review.” *ILR Review* 74 (1):3–26.
- Marinescu, Ioana and Daphné Skandalis. 2021. “Unemployment Insurance and Job Search Behavior.” *The Quarterly Journal of Economics* 136:887–931.
- Mercan, Yusuf and Benjamin Schoefer. 2020. “Jobs and Matches: Quits, Replacement Hiring, and Vacancy Chains.” *American Economic Review: Insights* 2 (1):101–24.
- Mongey, Simon and Giovanni Violante. 2019. “Macro Recruiting Intensity from Micro Data.” *NBER Working Paper* 26231 .
- Mueller, Andreas I, Damian Osterwalder, Zweimüller, and Andreas Kettemann. 2023. “Vacancy Durations and Entry Wages: Evidence from Linked Vacancy-Employer-Employee Data.” *The Review of Economic Studies* .
- Pissarides, Christopher. 2009. “The Unemployment Volatility Puzzle: Is Wage Stickiness the Answer?” *Econometrica* 77 (5):1339–1369.
- Pissarides, Christopher A. 2011. “Equilibrium in the Labor Market With Search Frictions.” *American Economic Review* 101 (4):1092–1105.
- Qiu, Xincheng. 2023. “Vacant Jobs.” Working Paper.

- Scur, Daniela, Raffaella Sadun, John Van Reenen, Renata Lemos, and Nicholas Bloom. 2021. "World Management Survey at 18: Lessons and the Way Forward." *IZA Discussion Paper* .
- Signorelli, Sara and Francois Fontaine. 2024. "Too Constrained to Grow. Analysis of Firms' Response to the Alleviation of Skill Shortages." Mimeo.
- Sorenson, Olav, Michael Dahl, Rodrigo Canales, and Diane Burton. 2021. "Do Startup Employees Earn More in the Long Run?" *Organization Science* 32 (3):587–604.
- Stantcheva, Stefanie. 2023. "How to Run Surveys: A Guide to Creating Your Own Identifying Variation and Revealing the Invisible." *Annual Review of Economics* 15:205–234.
- Sterk, Vincent, Petr Sedláček, and Benjamin Pugsley. 2021. "The Nature of Firm Growth." *American Economic Review* 111 (2):547–579.
- Terry, Ellie and Mels De Zeeuw. 2018. "How Do Firms Respond to Hiring Difficulties? Evidence from the Federal Reserve Banks' Small Business Credit Survey." FRB Atlanta Discussion Paper.
- Topa, Giorgio. 2011. "Labor Markets and Referrals." In *Handbook of Social Economics*, vol. 1. Elsevier, 1193–1221.

Online Appendix

A. Additional Tables and Figures

A.1. Tables

TABLE A.1. Hiring Obstacles and Aggregate Labor Market Conditions

Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Labor market tightness	0.09*** (0.02)	0.07*** (0.02)	0.07*** (0.02)	0.04* (0.02)	-0.01 (0.02)
<i>N</i>	2059	2059	2059	2059	2059
Unqualified hires	0.06*** (0.02)	0.06*** (0.02)	0.03 (0.02)	0.03 (0.02)	-0.04* (0.02)
<i>N</i>	2029	2029	2029	2029	2029
Unfilled vacancies	0.15*** (0.02)	0.07*** (0.02)	0.08*** (0.02)	0.05** (0.02)	-0.04 (0.02)
<i>N</i>	2029	2029	2029	2029	2029

Note: This table shows univariate OLS estimates of hiring obstacles from our survey on aggregate labor market conditions. Aggregate labor market conditions are measured at the occupational level from administrative data and are linked to our survey using the share of employment in a particular occupation at firm-level. The aggregate labor market conditions are converted to a Z-score. Asterisks indicate statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

TABLE A.2. Hiring Obstacles and Firm Characteristics: OLS regressions

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Size	0.03 (0.03)	-0.05** (0.03)	-0.07** (0.03)	-0.09*** (0.03)	-0.05** (0.03)
Age	-0.04 (0.03)	-0.03 (0.03)	-0.06** (0.03)	-0.07** (0.03)	-0.04 (0.03)
Productivity	0.02 (0.03)	-0.07*** (0.03)	-0.02 (0.03)	-0.05 (0.03)	-0.12*** (0.03)
Wage premium	-0.00 (0.03)	-0.07*** (0.02)	-0.02 (0.03)	0.01 (0.03)	-0.04 (0.03)
Local empl. share	-0.04 (0.03)	0.02 (0.03)	-0.09*** (0.03)	-0.02 (0.03)	-0.05** (0.02)
Wage floor	-0.19** (0.08)	-0.19** (0.08)	-0.00 (0.09)	-0.00 (0.09)	0.06 (0.09)
<i>N</i>	2059	2059	2059	2059	2059
Mean Dep. Var.	3.86	3.21	3.03	2.99	3.1
Adj.R2	0.054	0.049	0.049	0.036	0.082
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table shows OLS estimates of agreeing with different statements related to the question: "What factors can discourage the firm from recruiting despite the potential need?" The specifications are the same as in Table 3. The scale ranges from 1 (strongly disagree) to 5 (strongly agree). Asterisks report statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

TABLE A.3. Hiring Obstacles and Firm Characteristics: Unweighted Sample

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Size	0.73 (1.26)	-1.82 (1.23)	-2.99** (1.27)	-3.61*** (1.31)	-1.94 (1.20)
Age	-1.90* (1.14)	-1.90 (1.20)	-3.68*** (1.21)	-3.91*** (1.17)	-1.62 (1.18)
Productivity	0.76 (1.13)	-3.05** (1.19)	-0.47 (1.22)	-1.79 (1.18)	-4.73*** (1.28)
Wage premium	-0.05 (1.12)	-4.32*** (1.08)	-0.94 (1.04)	0.69 (1.02)	-2.53** (1.10)
Local empl. share	-1.05 (1.52)	0.36 (1.41)	-4.46*** (1.72)	-0.49 (1.64)	-2.16** (1.09)
Wage floor	-5.17 (3.50)	-10.30*** (3.68)	-1.81 (3.61)	-1.90 (3.49)	2.04 (3.80)
<i>N</i>	2059	2059	2059	2059	2059
Probability	.73	.37	.35	.33	.36
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table shows unweighted ordered probit estimates of agreeing with different statements related to the question: "What factors can discourage the firm from recruiting despite the potential need?" The specifications are the same as in Table 3. Asterisks indicate statistical significance at the 1, 5 and 10% level (***, **, *; respectively). Standard errors are in parentheses.

TABLE A.4. Hiring Obstacles and Firm Characteristics: Planned to Hire in 2020

Question: What factors can discourage the firm from recruiting despite the potential need?

Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Size	-0.62 (1.33)	-1.75 (1.79)	-3.76** (1.86)	-4.09** (1.96)	-1.22 (1.45)
Age	-2.62* (1.54)	-2.58 (1.80)	-1.22 (1.81)	-3.87** (1.79)	-2.14 (1.67)
Productivity	-0.37 (1.47)	-6.47*** (1.93)	-0.29 (1.82)	-3.57* (1.86)	-6.80*** (1.81)
Wage premium	1.94 (1.39)	-4.23*** (1.63)	-0.73 (1.48)	1.62 (1.44)	-1.19 (1.50)
Local empl. share	0.94 (1.60)	1.87 (2.56)	-2.46 (2.89)	-1.11 (2.88)	-2.89 (1.90)
Wage floor	-8.28* (4.68)	-8.40 (5.77)	-2.35 (5.75)	-0.24 (5.28)	11.61** (5.40)
<i>N</i>	1072	1072	1072	1072	1072
Probability	.73	.37	.35	.33	.36
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table shows ordered probit marginal effects of firm characteristics on the probability of agreeing with statements about different hiring obstacles. Only firms that indicate that they planned to hire in 2020 are included in the subsample. The exact wording of the hiring obstacles is cited in Section 3.1. Firm characteristics are measured from administrative data and are normalized (i.e., converted to a Z-score), except for whether the firm is covered by wage floors (indicator). Additional controls include firm, workforce, and respondent characteristics, as well as 59 industry- and 5 region-fixed effects, and firm-specific labor market tightness (see Section 2.4). Asterisks indicate statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

TABLE A.5. Hiring Obstacles and Firm Characteristics: Job Amenities

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Firm Characteristics					
Size	1.41 (1.35)	-1.84 (1.38)	-1.77 (1.53)	-1.81 (1.46)	0.27 (1.32)
Age	-2.86* (1.52)	-2.56 (1.62)	-4.16** (1.70)	-5.14*** (1.61)	-1.43 (1.59)
Productivity	1.85 (1.74)	-1.78 (1.89)	-1.42 (1.79)	-4.22** (1.91)	-6.04*** (2.10)
Wage premium	-3.55** (1.80)	-4.02** (2.00)	-2.48 (1.96)	-0.85 (1.91)	-2.81 (1.82)
Local empl. share	0.68 (1.73)	1.38 (1.59)	-5.53** (2.22)	-0.51 (1.78)	-2.98** (1.47)
Wage floor	-8.50 (5.23)	-7.42 (5.31)	-3.53 (5.45)	-2.37 (5.13)	3.80 (5.56)
Additional Pays					
Non standard condition (%)	-0.37 (1.25)	-0.12 (1.12)	2.46* (1.38)	-0.30 (1.52)	-2.92** (1.38)
Employee benefit (%)	1.50 (1.41)	1.03 (1.51)	-1.21 (1.69)	1.85 (1.34)	-0.37 (1.28)
<i>N</i>	1072	1072	1072	1072	1072
Probability	.73	.37	.35	.33	.36
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table shows the marginal effects of firm characteristics on the probability of agreeing with statements on hiring obstacles from ordered probit models. This sample only includes firms with information on non-standard employment conditions and employee benefits. The specifications are the same as in Table 3, except for two additional variables. Non-standard working conditions are the percentage of pay for non-standard working conditions, which includes irregular work schedules (such as night work, work on public holidays, delayed lunch, on-call and relocation) and irregular working conditions (such as outdoor work and extreme weather). Employee benefits are the percentage of pay for benefits, which is defined as the value of a free car, meals, lodging, multimedia, taxable health insurance and treatments, canteen arrangements, and work clothes. Asterisks indicate statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

TABLE A.6. Firms' Beliefs about the Unemployed and Poaching Rate

Q: What percentage of your employees are recruited from other firms?		
	(1)	(2)
Prefer to hire employed: loss of skill	10.41*** (1.95)	
Prefer to hire employed: ability		11.89*** (2.01)
<i>N</i>	2020	2020
Mean Dep. Var.	51.96	51.96
Adj.R2	0.143	0.147
Additional controls	Yes	Yes
Δ E -U abilities	Yes	Yes

Note: This table shows OLS estimates of the effect of firms' beliefs about hiring already employed workers over unemployed workers on their poaching rate. Column 1 includes beliefs in a loss skill during unemployment as a reason for preferring already employed workers. Column 2 includes the belief that the unemployed have lower abilities. Asterisks report statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

TABLE A.7. Hiring Obstacles, Firm Characteristics and Firm Preferences

Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles:	Skill shortage (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Prefer hiring employed	10.48*** (2.28)	9.00*** (2.38)	7.83*** (2.30)	7.29*** (2.21)	1.75 (2.23)
Firm Characteristics					
Size	1.56 (1.25)	-1.83 (1.31)	-2.63* (1.39)	-3.54** (1.44)	-1.74 (1.21)
Age	-2.41** (1.20)	-2.08 (1.28)	-3.14** (1.31)	-3.69*** (1.28)	-1.95 (1.25)
Productivity	0.82 (1.18)	-3.76*** (1.36)	-1.18 (1.34)	-2.19* (1.30)	-5.14*** (1.41)
Wage premium	0.15 (1.19)	-4.19*** (1.21)	-0.84 (1.17)	0.61 (1.11)	-2.42** (1.18)
Local empl. share	-1.23 (1.57)	0.55 (1.52)	-5.51*** (1.85)	-1.35 (1.73)	-2.41** (1.18)
Wage floor	-5.95* (3.58)	-8.81** (3.97)	-0.08 (3.98)	1.38 (3.81)	5.31 (4.07)
<i>N</i>	2031	2031	2031	2031	2031
Probability	.73	.37	.35	.33	.36
Additional controls	Yes	Yes	Yes	Yes	Yes
Δ E-U abilities	Yes	Yes	Yes	Yes	Yes

Note: The table shows ordered probit marginal effects of firm characteristics and firms' preferences for the employed over the unemployed on the probability of agreeing with statements about different hiring obstacles. It uses the exact same specification as Table 4 but, in addition, we report the estimates of the firm characteristics. Asterisks indicate statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

TABLE A.8. Hiring Obstacles, Firm Characteristics and Wage Inaccurate Beliefs

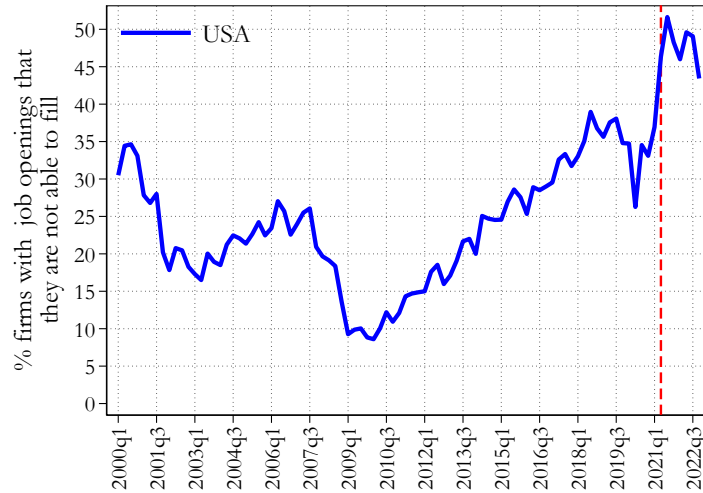
Question: What factors can discourage the firm from recruiting despite the potential need?					
Hiring obstacles: time	Skill shortage time (1)	Labor costs (2)	Search (3)	Training (4)	Uncertainty (5)
Underestimate own wage	-5.00* (2.88)	5.71* (2.94)	-1.95 (2.91)	-4.81* (2.76)	-0.22 (2.89)
Overestimate own wage	-0.37 (3.13)	-11.06*** (3.12)	3.64 (3.06)	1.26 (3.00)	-1.40 (3.04)
Firm Characteristics					
Size	1.33 (1.28)	-2.50* (1.34)	-2.84** (1.41)	-3.74*** (1.45)	-1.82 (1.21)
Age	-2.11* (1.19)	-2.03 (1.27)	-2.87** (1.29)	-3.49*** (1.25)	-1.66 (1.24)
Productivity	1.16 (1.20)	-3.40** (1.33)	-0.94 (1.32)	-2.04 (1.30)	-4.99*** (1.39)
Wage premium	1.11 (1.72)	-8.33*** (1.64)	0.53 (1.63)	2.08 (1.57)	-2.54 (1.67)
Local empl. share	-1.05 (1.55)	0.53 (1.54)	-5.37*** (1.89)	-0.95 (1.77)	-2.52** (1.18)
Wage floor	-7.37** (3.58)	-9.75** (3.93)	-0.83 (3.90)	0.00 (3.76)	3.97 (4.03)
<i>N</i>	2059	2059	2059	2059	2059
Probability	.73	.37	.35	.33	.36
Additional controls	Yes	Yes	Yes	Yes	Yes

Note: The table shows ordered probit marginal effects of firm characteristics and wage inaccurate beliefs on the probability of agreeing with statements about different hiring obstacles. It uses the same specification as Table 5, but this table shows the estimates of the firm characteristics. Asterisks indicate statistical significance at the 1, 5 and 10% level (***, **, * respectively). Standard errors are in parentheses.

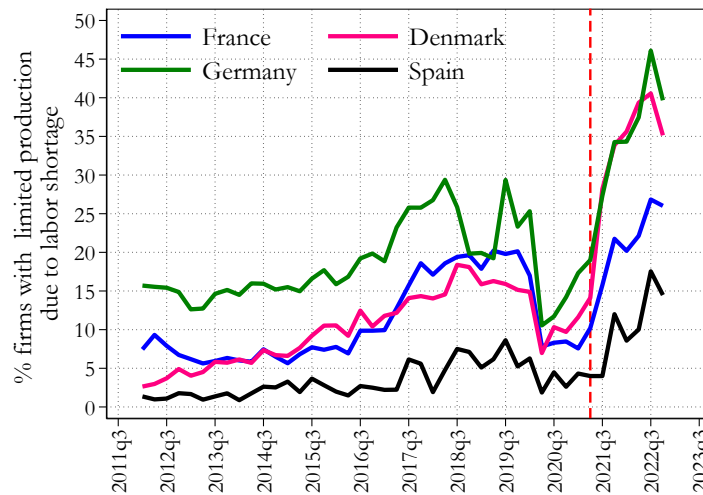
A.2. Figures

FIGURE A.1. The Prevalence of Hiring Difficulties Across Countries

Panel (a): Evidence from the United States

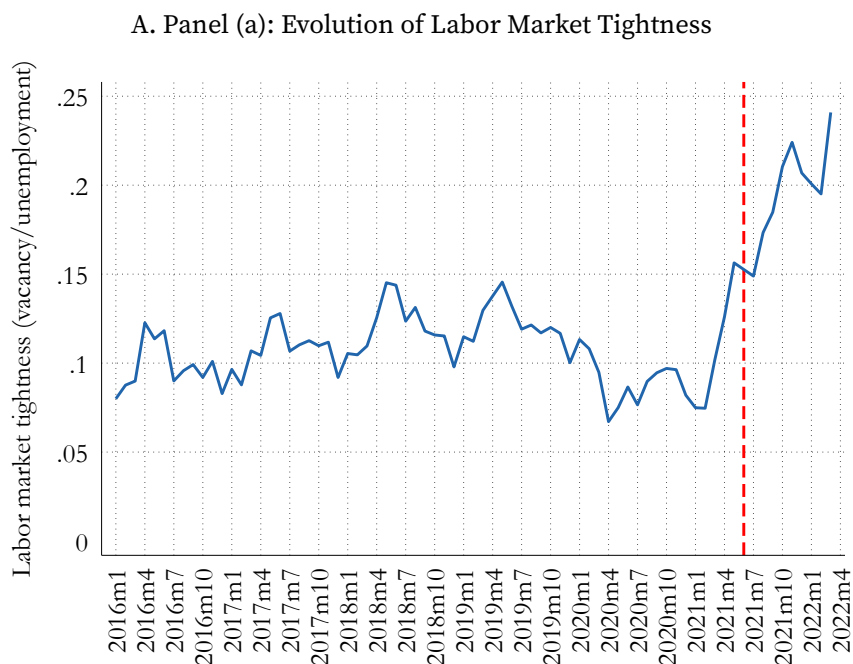


Panel (b): Evidence from Selected European Countries



Note: The dotted red line indicates the time (June 2021) when the survey was conducted. Panel (a) reports the response to the question: Do you have any job openings that you are not able to fill right now? Source: Small Business Economic Trends, NFIB. Panel (b) reports the percentage of firms with limited production due shortage of labor in selected European countries. The question is: What main factors are currently limiting your production? Possible responses are: none, insufficient demand, shortage of labor force, shortage of material and/or equipment, financial constraints, other factors. Source: Business Survey from the DG-ECFIN 2022, i.e., the European Commission Department for Economic and Financial Affairs.

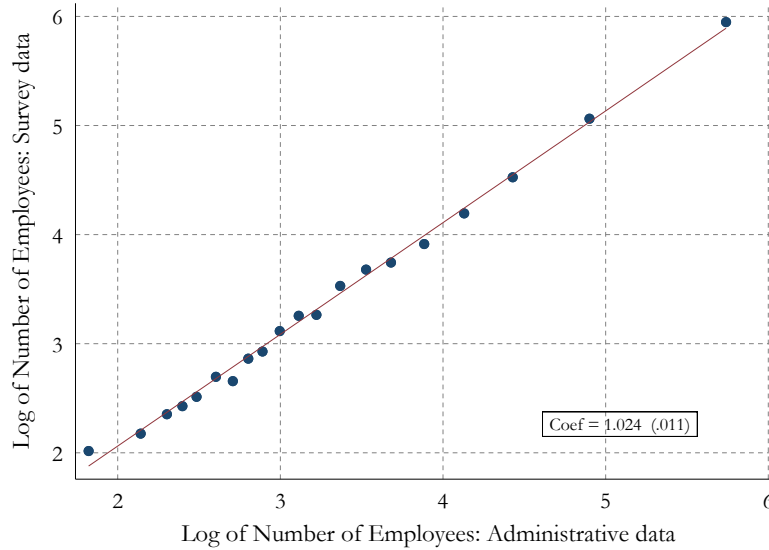
FIGURE A.2. Economic Context around the time of the Survey Implementation



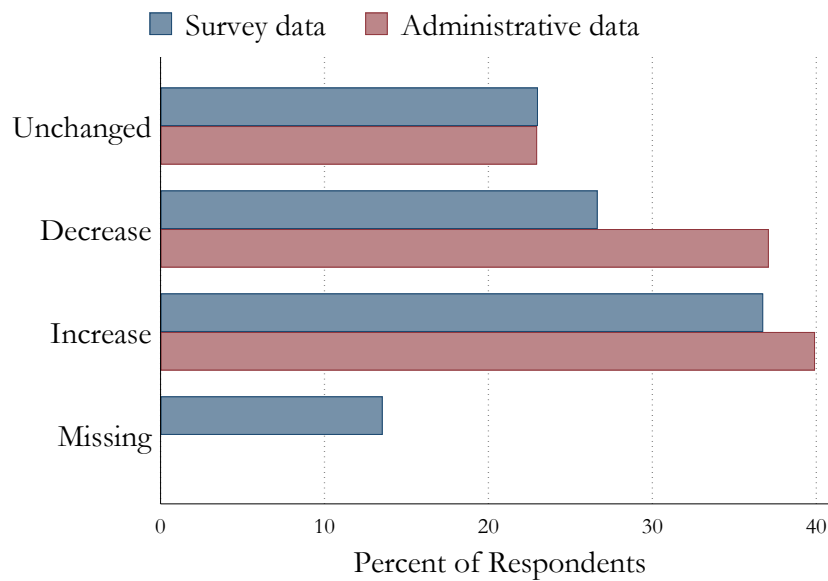
Note: This figure reports the number of vacant positions over the number of unemployed workers in Denmark. The dotted red line indicates the time (June 2021) when the survey was conducted. Source: STAR.

FIGURE A.3. Comparison of Survey and Administrative data

A. Panel (a): Number of Employees

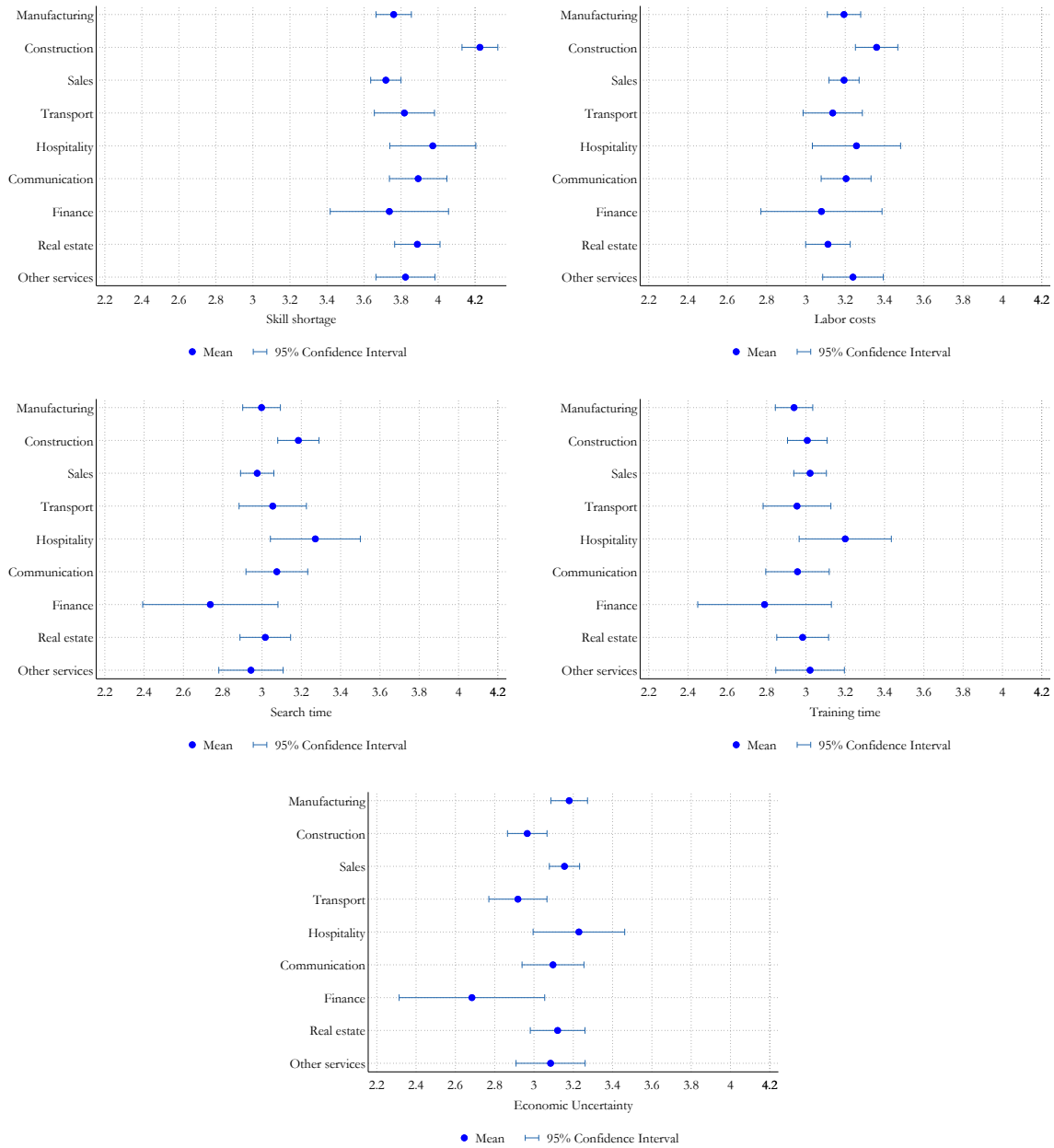


B. Panel (b): Revenue change



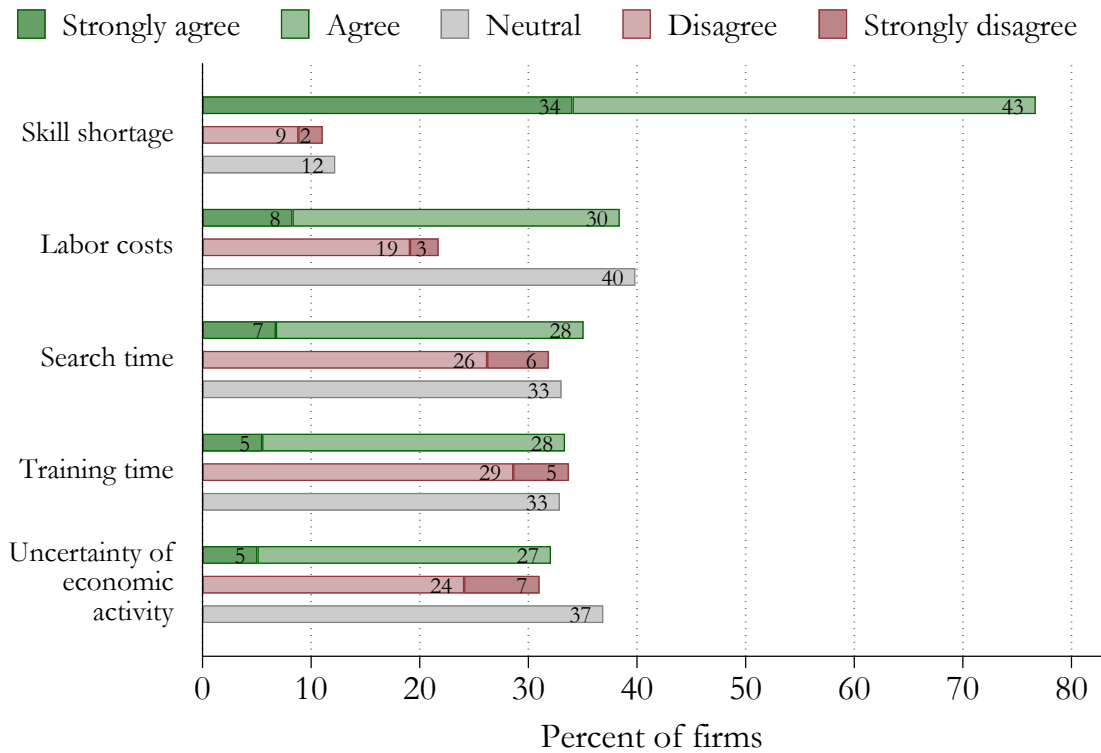
Note: Panel (a) compares the survey question, "How many employees were there in the company on May 1, 2021?" to the number of employees in March 2021 in the matched employer-employee dataset (BFL). Both variables are in logs and are winsorized. Panel (b) compares revenue changes from 2019 to 2020, in the survey and in the firm's financial data (FIRM).

FIGURE A.4. Hiring Obstacles by Sector



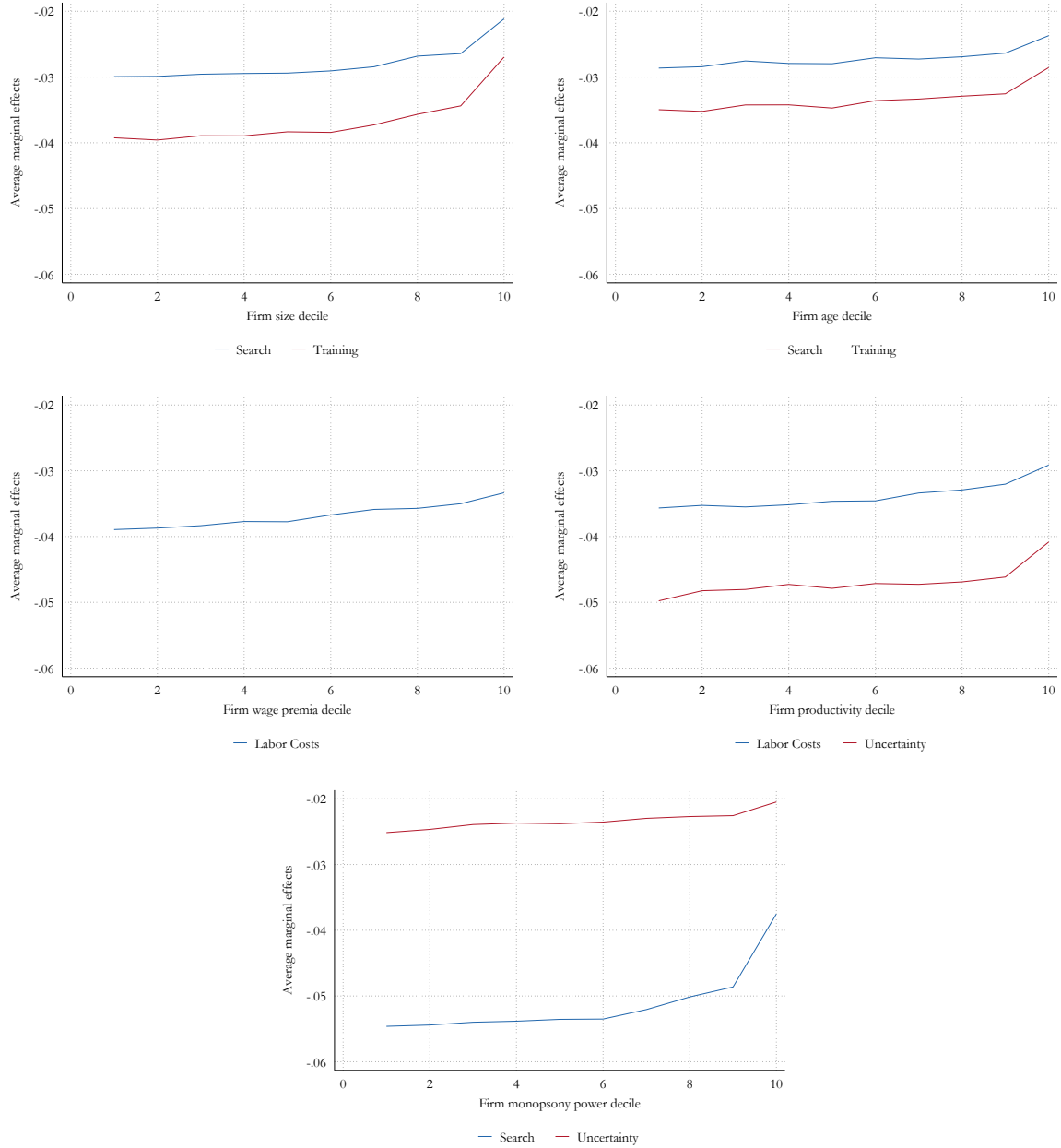
Note: These figures show how hiring obstacles (skill shortage, labor costs, search time, training time, economic uncertainty) vary by industry. The scale ranges from 1 to 5, where 5 stands for "strongly agree" and 1 stands for "strongly disagree". We report the mean responses and the 95 percent confidence intervals for each industry.

FIGURE A.5. Hiring Obstacles for Firms that Planned to Hire in 2020



Note: The figure reports responses to the question: What factors can discourage the firm from recruiting despite the potential need? The hiring obstacles are: The lack of qualified candidates (Skill shortage); Job seekers want a higher wage than the firm can offer (Labor costs); Finding and choosing the right employee is too time-consuming (Search time); Training employees in firm-specific skills is too time-consuming (Training time); The uncertainty of economic activity. Only firms that indicate that they planned to hire in 2020 after the pandemic started are included in the sample.

FIGURE A.6. Marginal Effects By Decile of Firm Characteristics



Note: These figures report the average marginal effects of firm size, age, wage premium, productivity and labor market power on firms' probability of agreeing with statements about hiring difficulties. Only statements that are strongly correlated with the specific firm characteristics are included(see Table 3). The marginal effects are the average marginal effects (evaluated at the observational level) of each decile.

B. Additional Information on Data

B.1. Information about Administrative and Survey Data Linked to Our Survey

Most datasets can be obtained by contacting the Research service (*Forskningsservice*) of Denmark Statistics (DST henceforth). The administrative datasets come from various sources gathered by the National Statistics Agency (Statistics Denmark), the National Employment Policy Agency (STAR), and the largest employer association in Denmark (DA). To our knowledge, datasets provided by DST do not contain a DOI number, complicating replicability. The datasets that are used are recorded at a yearly frequency. Establishment identifiers are available, but our analysis focuses on the legal unit firm identifier (CVR number) as our survey asks questions about firms' practices. Individual identifiers are anonymized social security numbers (PNR number). The identifiers do not change over time. Below, we provide information about the different sources we use in this paper.

Information about workers. We use several datasets to collect information about workers. The first dataset is called IDAP (*IDA persondata*). IDAP contains information about the total population in Denmark. The status information for individuals mainly refers to the end of the year (31 December). From this dataset, we retrieve information about workers' age, gender, and socioeconomic status. The social economic status information allows us to delete self-employed, apprentices, and students to estimate the AKM model. It also enables to classify workers as employed or unemployed. The second dataset is called IDAN (*IDA ansættelser*). From this dataset, we retrieve information about occupation, earnings, hours worked, and firm identifier. Recall that hours worked are defined as paid hours (at the worker-firm frequency) that include contractual and overtime hours. Earnings are defined as the near-universe of taxable income. We use information from this dataset to define the dominant job and estimate the AKM model. Occupation classification follows the ISCO classification at 6-digit frequency.

Information about firms. We use the General Company Statistics called the FIRM dataset, which annually lists active companies in Denmark. FIRM is built from several Statistics Denmark registers. FIRM covers economic and employment information about all sectors and industries. Active companies are defined as companies with at least 0.5 full-time hours of work. The firm identifier is the CVR number, the legal firm identifier

in Denmark. We use this dataset to retrieve information about the industry classification (NACE) and the regional classification (NUTS).

The register that is used in FIRM for the value-added variable is the Accounts statistics for the Non-Agricultural Private Sector (Regnskabsstatistikken for private byerhverv), abbreviated APB.⁴¹ APB only includes market activity and does not contain agriculture, fishing, ports, banks, insurance, public housing companies, or public administration. There is a data break in 2014 in the population of firms included in APB. Since 2014, firms in utilities, regional and long-distance trains, and radio and TV stations have been included. Value added is defined using several items from the income statement (*Resultatopgørelse*). These items are: sales and other operating income - cost of materials and equipment - costs of energy and subcontractors - rent paid - payments to temporary workers and operational leasing of goods, and ordinary write-offs and other external charges.

Poaching rate. We use the BFL register to construct the poaching rate. BFL is a matched employer-employee data recording, at monthly frequency, the start and end dates of a job spell, as long as occupation codes, total earnings, and total hours worked in a given establishment. We measure $Poaching_j = \frac{H_{jt}^{EE}}{H_{jt}}$ where j is a firm and H_{jt}^{EE} is the number of new hires coming from other firms, and H_{jt} is all new hires (excluding recalls) by the firm. This definition is standard in the literature, see, e.g, Bagger and Lentz (2019).

Routine task index. We use the following categories of jobs based on tasks. We follow Acemoglu and Autor (2011) and use composite measures of O*NET Work Activities and Work Context Importance scales. Instead of using offshorability directly, we use three components of the offshorability composite measure to define "Social interaction". Below we list the definition of the variables we use.

Non-routine cognitive: Analytical.

- Analyzing data/information
- Thinking creatively
- Interpreting information for others

Non-routine cognitive: Interpersonal.

⁴¹This register is itself built from several sources: questionnaires, official annual accounts submitted in XBRL format to the Danish Business Authority (*Erhvervsstyrelsen*), the Danish Tax Authority (SKAT), Denmark's Statistics Business Register, and the Danish Medicines Agency (*Lægemiddelstyrelsen*).

- Establishing and maintaining personal relationships
- Guiding, directing and motivating subordinates
- Coaching/developing others

Routine cognitive

- Importance of repeating the same tasks
- Importance of being exact or accurate
- Structured v. Unstructured work (reverse)

Routine manual

- Pace determined by speed of equipment
- Controlling machines and processes
- Spend time making repetitive motions

Non-routine manual: physical

- Operating vehicles, mechanized devices, or equipment
- Spend time using hands to handle, control or feel objects, tools or controls
- Manual dexterity
- Spatial orientation

Non-routine manual: interpersonal adaptability

- Social perceptiveness

Social interaction

- Face-to-face discussions
- Assisting and caring for others
- Performing for or working directly with the public

TABLE A.9. Definition of Variables

Variable:	Definition and construction:	Dataset:	Variable name:
<i>Firm characteristics</i>			
Firm size	Number of employees (full-time equivalent, FTE)	BFL	AJO_LOENTTIMER
Firm age	Number of years since firm creation	FIRM	JUR_FRA_DATO
Productivity	Value added per firm size	FIRM	
Wage premiums	AKM firm fixed effects	IDAN	
Local. emp. share	Firm's employment divided by total employment within a given region-industry	FIRM	GF_ANSATTE
Wage floors	=1 if at least 50% of employees are subject to a wage floor set at the industry-occupation level in the firm	DA	---
Industry	59 industries codes (2-digit NACE)	FIRM	GF_NACE2_DB07
Region	5 Danish regions codes (2-digit NUTS)	FIRM	JUR_BEL_REGION_KODE
Job growth	Net job creation rate from 2019 to 2020	BFL	AJO_LOENTTIMER
Capital stock	Fixed assets (e.g, buildings, machines, patents)	FIRM	GF_AAT
Liquidity	Liquid assets (e.g., cash, bonds)	FIRE	VKT
Revenue growth	Revenue growth from 2019 to 2020	FIRM	GF_OMS
Routine task index	$RTI_k = \ln(T_k^R) - \ln(T_k^M) - \ln(T_k^A)$	O*NET	
Poaching rate	Fraction of new hires with less than two weeks of non-employment spells between two firms	BFL	
<i>Workforce characteristics</i>			
Education	% of workers with at least a bachelor's degree	UDDA	HFAUDD
Female	% of females in the firm	IDAP	KON
Unionization	% unionized workers in the firm	IND	FAGFKD
Upskilling	Mean education of new hires in 2020 / Mean education of new hires in 2019	UDDA	HFAUDD
Age	Mean age in the firm	IDAP	ALDERNOV
Tenure	Mean tenure in the firm	IDAN	ANSAAR
Benefits	Percentage of salary paid as personal benefits (e.g, car, meals, accommodation)	LONN	PERSGODE_PRAE
Non-standard work conditions	Percentage of salary paid as compensation for non-standard conditions (e.g, outside working hours)	LONN	GENE_PRAE
<i>Labor market characteristics</i>			
$\Delta E - U$	Diff. in AKM worker fixed effects among employed and unemployed: $\Delta_{E-U,j} = \sum_{o=1}^O w_{oj} (\bar{\alpha}_o^E - \bar{\alpha}_o^U)$	IDAN	ANSAAR
Tightness	Firm-level labor market tightness: $\theta_j = \sum_{o=1}^O w_{oj} \theta_o$ with $\theta_o = \#V_o / \#U_o$ and $w_{oj} = N_{oj} / N_j$	STAR	---
Unfilled vacancies	Similar to θ_j , but use % of unfilled vacancies in an occupation instead of θ_o	Rekrutteringssurvey	
Unqualified hires	Similar to θ_j , Use % of filled vacancies with "unqualified" hires in an occupation instead of θ_o	Rekrutteringssurvey	
HHI	HHI index for employment at the local labor market level (i.e region-industry)	FIRM	GF_ANSATTE

Note: The table reports the administrative datasets and the variables that we use as the firm characteristics and additional controls in our estimates. All variables are measured in 2019 unless otherwise specified.

FIGURE A.7. Invitation Letter to Participate in the Survey



Att.: Den administrerende direktør

Hvordan kommer dit firma styrket ud af krisen?

Rambøll gennemfører på vegne af Københavns Universitet en spørgeskemaundersøgelse, der skal belyse, hvordan virksomheder kan komme styrket ud af Covid19-krisen. Vi spørger om hvad du/I har gjort for at komme igennem krisen og hvilke overvejelser du gør om tiden efter Covid19.

Projektet gennemføres under ledelsen af Niels Bohr Professor Morten Bennedsen, Økonomisk Institut, og er støttet af blandt andet Industriens Fond og det Samfundsvidenskabelige Forskningsråd.

Hvis du ønsker det, vil du efter undersøgelsens afslutning modtage en anonymiseret benchmarkingsrapport, hvor du kan se dine besvarelser op mod fordelingen af andre besvarelser. Vi overholder naturligvis alle databeskyttelsesreglerne.

Det tager ca. 20 minutter at udfylde spørgeskemaet. Undervejs kan du lukke skemaet og senere genoptage besvarelsen via linket, som du har modtaget her. Husk derfor at gemme denne invitation, til du har afsluttet din besvarelse.

Sådan gør du

Spørgeskemaet besvares elektronisk via internettet. Du kan svare på alle computere, tablets (f.eks. iPad m.m.) og smartphones. Du får adgang til dit personlige spørgeskema ved at klikke på nedenstående link:

<https://surveys.ramboll.com/answer?key=ZNEVCQ9MSJ1Y>

Vi vil bede dig besvare spørgeskemaet senest **den 27. juni 2021**.

Du er sikret fortrolighed

Dine svar behandles fortroligt af Rambøll og vil kun fremgå i anonymiseret form. Du kan få mere information om behandling af personoplysninger i forbindelse med undersøgelsen på forsiden af spørgeskemaet.

Kontakt

Hvis du har yderligere spørgsmål, er du velkommen til at kontakte Rambøll på e-mail: skemasupport@ramboll.com eller tlf. 6915 8076 på hverdage i tidsrummet kl. 8.00-16.00.

På forhånd tak for din deltagelse!

Med venlig hilsen
Rambøll og
Københavns Universitet

Note: The figure shows the invitation letter that firms received in an email asking them to participate in the survey. See an English translation of the letter below.

Att: The Administrative Director

How does your company come out of the crisis stronger?

On behalf of the University of Copenhagen, Rambøll is carrying out a survey to shed light on how firms can emerge stronger from the COVID19 crisis. We ask what you/you and others have done to get through the crisis and what thoughts you have about the time after COVID19.

The project is carried out under the leadership of Niels Bohr Professor Morten Bennedsen, Department of Economics, University of Copenhagen, and is supported by, among others Industriens Fond and the Social Science Research Council.

If you participate in the survey, we will offer you an anonymized benchmarking report that shows your responses against the distribution of the other responses. We naturally comply with all data protection regulations.

It takes approximately 20 minutes to complete the questionnaire. You can close the form and resume it later by again clicking on the link below. Therefore, please remember to save this invitation until you have completed the survey.

Here's how you do it

The questionnaire is answered electronically via the Internet. You can complete the questionnaire on any computer, tablet (e.g. iPad, etc.) or smartphone.

To access your personal questionnaire, click on the link below: [LINK](#)

We ask that you complete the questionnaire no later than 27 June 2021.

You are guaranteed confidentiality

Your answers are treated confidentially by Rambøll and will only appear in anonymized form. You can find more information about the treatment of personal data in connection with the survey on the front page of the questionnaire.

Contact

If you have further questions, please feel free to contact Rambøll by e-mail: skemasupport@ramboll.com or tel. 6915 8076 on weekdays between 8.00-16.00.

Thank you in advance for your participation

Yours sincerely

Rambøll and University of Copenhagen

B.2. The Survey Questionnaire

This section reports the questions from our survey we use in this paper. While some phrases can seem uncommon in English, they are perfectly understandable in Danish. Key phrases and Danish words are reported in parenthesis in Danish.

Background question.

- What is your role in the company?
 - Owner manager
 - Director without ownership
 - Board member without ownership
 - Owner without being a board member
 - Other

All categories but "Other" are combined in this question to create the variable "Manager respondents".

- Does a person or family have 50% or more of the ownership?
 - Yes
 - No
 - Do not know

The category "Yes" in this question corresponds to the variable "Family-owned firm".

- How many employees were there in the company on May 1, 2021? Note: Include all employees, including full-time, part-time, furloughed and employees on apprenticeships and parental leave. Give your best estimate.
 - _____

- How much did revenue (*omsætningen*) change in 2020 compared to 2019? Note: If you do not know the exact change, give your best estimate.

- Reduced by 100 percent
- Reduced (indicate the percentage): _____
- Unchanged
- Increased (indicate the percentage): _____
- Increased by 100 percent or more

- Is the company primarily a subcontractor (*underleverandør*) to other companies?
 - Yes, for 90 percent or more of the revenue
 - Yes, for 50 percent to 89 percent of the revenue
 - Yes, for 25 percent to 49 percent of the revenue
 - Yes, for 10 percent to 24 percent of the revenue

- Yes, for less than 10 percent of the revenue
- No
- Do not know

The categories "Yes, for 90 percent or more of the revenue" and "Yes, for 50 percent to 89 percent of the revenue in this question corresponds to the variable "Subcontractor".

- In the following questions, we ask about pay (*løn*)⁴² and hiring practices (*ansættelsespraksis*). How close are you to such decisions?
 - I am responsible for pay and employment conditions
 - I am not responsible, but I know about pay and employment conditions
 - I only know a little about pay and employment conditions

- Do you think that this company offers lower or higher salaries than competing companies in your industry? Competing companies are other employers that hire people with the same skills in your region. If you are not sure, please come up with an estimate.
 - Much lower
 - Lower
 - About the same
 - Higher
 - Much higher

Hiring question.

- What percentage of your employees are recruited from other firms? Recruited employees from other firms means people who were already employed and not unemployed or had not just entered the labor market. If you are not sure, come up with your best guess.
 - 0% from other firms
 - 10%
 - 20%
 - 30%
 - 40%

⁴²In Danish, the word *løn* is usually translated as salary, pay or wages. The definition in the dictionary ordnet.dk is "payment that an employee receives for working".

- 50%
- 60%
- 70%
- 80%
- 90%
- 100%, all from other firms
- Tell us your thoughts about hiring other firms' employees. Please express your opinion on the following statements. Respondents have five options (strongly agree, agree, neutral, disagree, and strongly disagree).
 - We do not necessarily prefer candidates who are employed, as there is still a need for company-specific qualities and training.
 - We do not necessarily prefer candidates who are employed as we are in doubt as to why an applicant wants to change jobs.
 - We prefer to hire candidates who are employed as unemployed workers lose their skills.
 - We prefer to hire candidates who are employed because unemployment workers have lower abilities than those who are employed.
 - Other, please write.
- When recruiting an employee, which part of the hiring process is most costly in time or money?
 - Search for candidates, conducting interviews
 - Briefing of new employees (either through his / her manager or colleagues)
- What factors can discourage the firm from recruiting despite the potential need? Please express your opinion on the following statements. Respondents have five options (strongly agree, agree, neutral, disagree, and strongly disagree).
 - The lack of qualified candidates.
 - Candidates typically want a higher salary than what the firm can offer.
 - Finding and choosing the right employee is too time consuming
 - Training (*Orientering og træning*) with company-specific skills (*evner*) and knowledge (*viden*) takes too much time
 - The uncertainty of economic activity
 - Other, please write.
- When will the newly hired employee achieve/have achieved the same productivity as an average employee in a similar position? Please indicate the estimate in months. The possible options are from within one month up to 18 months (or more).

C. Search And Matching Model

The following model illustrates the results we derive in our empirical analysis. The model is a search and matching model that is similar in many aspects to the theoretical framework developed in Cahuc, Carcillo, and Le Barbanchon (2019). We assume that time is discrete and that firms produce differentiated products using labor as the only input factor in the production function. In period t the firm produces using the production function $A_t \frac{L_t^{1-\alpha}}{1-\alpha}$, where A_t is productivity in period t , L_t is labor in the same period and α combines both the labor elasticity of the production and the price elasticity of the production function.

For simplicity, we keep separation and the wage decisions exogenous. Posting vacancies costs c units of output per period. An exogenous fraction of workers, q_{t-1} , leaves the firm and firms post vacancies. After that, workers are hired, where matching happens with probability $m_t(\theta_t) = \bar{m}\theta_t^{-\mu}$, where $\bar{m} > 0$, $\theta_t = V_t/U_{t-1}$ is labor market tightness, V_t is the number of vacancies in period t and U_{t-1} is the number of unemployed workers in period $t-1$. The job remains vacant at the rate $1 - m_t$. Finally, production takes place.

The value of the firm is:⁴³

$$\Pi(A_t, w_t, m_t, q_{t-1}, L_{t-1}) = \max_{V_t} A_t \frac{L_t^{1-\alpha}}{1-\alpha} - w_B L_t - cV_t + \beta \Pi(A_{t+1}, w_{t+1}, m_{t+1}, q_t, L_t),$$

subject to the evolution of employment

$$L_t = (1 - q_{t-1}) L_{t-1} + m_t V_t$$

Consider two different states of nature, A_B when there is a boom, and A_R during a recession, hence $A_B > A_R$. The transition probability from state A_B to state A_R is denoted e_B , while the transition probability from state A_R to state A_B is denoted e_R . The separation rates potentially differ in the two states:

$$\begin{aligned} \Pi^B(L_{t-1}) &= \max_{V_t} \left[A_B \frac{L_t^{1-\alpha}}{1-\alpha} - w_B L_t - cV_t + \beta \left(e_B \Pi^R(L_t) + (1 - e_B) \Pi^B(L_t) \right) \right], \\ \Pi^R(L_{t-1}) &= \max_{V_t} \left[A_R \frac{L_t^{1-\alpha}}{1-\alpha} - w_R L_t - cV_t + \beta \left(e_R \Pi^B(L_t) + (1 - e_R) \Pi^R(L_t) \right) \right], \end{aligned}$$

⁴³The detailed solution of the firm's problem is available upon request.

subject to the evolution of employment

$$L_t = (1 - q_j) L_{t-1} + m_t V_t, j = B, R,$$

where q_j is the separation rate and we let $q_R > q_B$.

After several manipulations the first order conditions in steady state are⁴⁴

$$(A.1) \quad A_B L_B^{-\alpha} = w_B - \beta e_B (1 - q_R) \frac{c}{\bar{m}} \theta_R^\mu + \frac{c}{\bar{m}} \theta_B^\mu (1 - \beta(1 - e_B)(1 - q_B)),$$

$$(A.2) \quad A_R L_R^{-\alpha} = w_R - \beta e_R (1 - q_B) \frac{c}{\bar{m}} \theta_B^\mu + \frac{c}{\bar{m}} \theta_R^\mu (1 - \beta(1 - e_R)(1 - q_R)),$$

The law of motion equations are:

$$(A.3) \quad q_j L_j = \bar{m} \theta_j^{-\mu} V_j \frac{U_j}{U_j} = \bar{m} \theta_j^{-\mu} \frac{V_t}{U_j} U_j = \bar{m} \theta_j^{1-\mu} (1 - L_j), j = B, R.$$

Hence, the equations, A.1-A.3 determine labor market tightness and labour demand in booms and recessions $\theta_B, \theta_R, L_B,$ and L_R . We assume that parameter values are such that labor market tightness is higher in a boom than in a recession, $\theta_B > \theta_R$ corresponding to higher employment, which is consistent with the data.

Comparative statics. We consider how labor demand and labor market tightness are affected by the variables considered in Figure 1 and Table 3. We assume that this is in a recession state (R).

First, we consider the impact of skill shortage on labor supply. We illustrate this effect by letting the productivity of workers fall corresponding to a lower productivity of the workers firms potentially hire, $\Delta A_R < 0$.

After several steps⁴⁵ we obtain:

⁴⁴Note that we disregard the transition periods between states. This gives two levels of employment, L_B and L_G ; and 2 levels of labor market tightness, θ_B and θ_R .

⁴⁵That is, differentiation (A.2) and (A.3) with respect to θ_R, L_R and A_R , and using using equation (A.5) in (A.4).

$$(A.4) \quad dA_R L_R^\alpha - A_R \alpha L_R^{-\alpha-1} \frac{dL_R}{d\theta_R} d\theta_R = \frac{c}{\bar{m}} \mu \theta_R^{\mu-1} d\theta_R (1 - \beta(1 - e_R)(1 - q_R)),$$

$$(A.5) \quad \frac{dL_R}{d\theta_R} = \frac{\bar{m} \left((1 - \mu) \theta_R^{-\mu} (1 - L_j) \right)}{\left(q_R + \bar{m} \theta_R^{1-\mu} \right)}.$$

$$(A.6) \quad \frac{d\theta_R}{dA_R} \Delta A_R = \frac{L_R^\alpha}{\frac{c}{\bar{m}} \mu \theta_R^{\mu-1} + A_R \alpha L_R^{\alpha-1} \frac{\bar{m} \left((1 - \mu) \theta_R^{-\mu} (1 - L_j) \right)}{\left(q_R + \bar{m} \theta_R^{1-\mu} \right)}} \Delta A_R < 0,$$

where, therefore, $\frac{dL_R}{dA_R} \Delta A_R < 0$ and $\frac{d\theta_R}{dA_R} \Delta A_R < 0$. The expected sign is therefore negative, which is consistent with the findings in Figure 1 and Table 3. Hence, skill shortage implies fewer vacancies supplied and lower employment.

Second, we consider the labor costs as an impediment to hiring workers, which corresponds to a higher wage, which we observe in the second row in Figure 1. The impact on labor market tightness and employment is:

$$(A.7) \quad -A_R L_R^{\alpha-1} \frac{dL_R}{d\theta_R} d\theta_R = dw_R + \frac{c}{\bar{m}} \mu \theta_R^{\mu-1} d\theta_R (1 - \beta(1 - e_R)(1 - q_R)),$$

Using equation (A.5) we obtain

$$(A.8) \quad \frac{d\theta_R}{dw_R} \Delta w_R = - \frac{1}{\frac{c}{\bar{m}} \mu \theta_R^{\mu-1} + A_R \alpha L_R^{\alpha-1} \frac{\bar{m} \left((1 - \mu) \theta_R^{-\mu} (1 - L_j) \right)}{\left(q_R + \bar{m} \theta_R^{1-\mu} \right)}} \Delta w_R < 0.$$

Hence, higher labor costs lead to fewer hirings, and labor market tightness and employment falls, $\frac{dL_R}{dw_R} \Delta w_R < 0$ and $\frac{d\theta_R}{dw_R} \Delta w_R < 0$.

Third, the third row in Figure 1, the impact of search time, can be considered through a change in the match efficiency parameter \bar{m} . We differentiate with respect to θ_R , L_R and \bar{m} . First, we obtain from equation (A.2) after using the equation to show:

$$(A.9) \quad A_R \alpha L_R^{-\alpha-1} dL_R + \frac{c}{\bar{m}} \mu \theta_R^{\mu-1} (1 - \beta(1 - e_R)(1 - q_R)) d\theta_R = \frac{1}{\bar{m}} (A_R L_R^{-\alpha} - w_R) d\bar{m},$$

Then differentiating equation (A.3) gives

$$(A.10) \quad dL_R \left(q_R + \bar{m} \theta_R^{1-\mu} \right) - \bar{m} \left((1 - \mu) \theta_R^{-\mu} (1 - L_j) \right) d\theta_R = \theta_j^{1-\mu} (1 - L_j) d\bar{m},$$

These two equations have to be determined simultaneously and since the determinant is negative, $D < 0$, if search time increases, that is, $\Delta \bar{m} < 0$, then we obtain

$$(A.11) \quad \frac{dL_R}{d\bar{m}} \Delta \bar{m} = \frac{-\bar{m} \left((1 - \mu) \theta_R^{-\mu} (1 - L_j) \right) - \frac{c}{\bar{m}} \mu \theta_R^{\mu-1} (1 - \beta(1 - e_R)(1 - q_R))}{D} \Delta \bar{m} < 0.$$

$$(A.12) \quad \frac{d\theta_R}{d\bar{m}} \Delta \bar{m} = \frac{-\left(q_R + \bar{m} \theta_R^{1-\mu} \right) + A_R \alpha L_R^{-\alpha-1}}{D} \Delta \bar{m},$$

Thus, longer search time leads to lower employment.

Fourth, the fourth row in Figure 1, increased uncertainty, we can illustrate by a reduction in the transition from a recession into a boom, that is, e_R falls, which means that the duration of a recession, $1/e_R$, increases. We differentiate the FOC in the recession state and get:

$$(A.13) \quad -A_R \alpha L_R^{-\alpha-1} \frac{dL_R}{d\theta_R} d\theta_R = \frac{c}{\bar{m}} \mu \theta_R^{\mu-1} d\theta_R (1 - \beta(1 - e_R)(1 - q_R)) - \frac{c}{\bar{m}} \beta \left((1 - q_B) \theta_B^\mu - \theta_R^\mu (1 - q_R) \right) de_R,$$

and then use equation (A.5) to get:

$$(A.14) \quad \frac{d\theta_R}{de_R} \Delta e_R = \frac{\frac{c}{\bar{m}} \beta \left((1 - q_B) \theta_B^\mu - \theta_R^\mu (1 - q_R) \right)}{\frac{c}{\bar{m}} \mu \theta_R^{\mu-1} + A_R \alpha L_R^{-\alpha-1} \frac{\bar{m} \left((1 - \mu) \theta_R^{-\mu} (1 - L_j) \right)}{\left(q_R + \bar{m} \theta_R^{1-\mu} \right)}} \Delta e_R < 0,$$

which is negative as $(1 - q_B) \theta_B^\mu > \theta_R^\mu (1 - q_R)$. Hirings and employment are expected to

fall.

Finally, we consider the impact of longer training time. We illustrate this by considering the impact of a higher c . We differentiate equation (A.2) and use it again to substitute to simplify to obtain:

$$(A.15) \quad -A_R \alpha L_R^{-\alpha-1} \frac{dL_R}{d\theta_R} d\theta_R = \frac{c}{\bar{m}} \mu \theta_R^{\mu-1} d\theta_R (1 - \beta(1 - e_R)(1 - q_R)) - \frac{1}{\bar{m}} (A_R L_R^{-\alpha} - w_R) dc,$$

and then use equation (A.5) to obtain if $\Delta c > 0$:

$$(A.16) \quad \frac{d\theta_R}{dc} \Delta c = - \frac{\frac{1}{\bar{m}} (A_R L_R^{-\alpha} - w_R)}{\frac{c}{\bar{m}} \mu \theta_R^{\mu-1} + A_R \alpha L_R^{\alpha-1} \frac{\bar{m} \left((1-\mu) \theta_R^{-\mu} (1-L_j) \right)}{(q_R + \bar{m} \theta_R^{1-\mu})}} \Delta c < 0,$$

Hence, hirings and employment are expected to fall when training costs increases: $\frac{dL_R}{dc} \Delta c < 0$ and $\frac{d\theta_R}{dc} \Delta c < 0$.

References

- Acemoglu, Daron and David Autor. 2011. "Skills, tasks and technologies: Implications for employment and earnings." *Handbook of labor economics* 4:1043–1171.
- Bagger, Jesper and Rasmus Lentz. 2019. "An Empirical Model of Wage Dispersion With Sorting." *The Review of Economic Studies* 86 (1):153–190.
- Cahuc, Pierre, Stephane Carcillo, and Thomas Le Barbanchon. 2019. "The Effectiveness of Hiring Credits." *The Review of Economic Studies* 86 (2):593–626.